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Types of some of the vehicles tested in the research reported in this magazine on Braking Performance of Motor Vehicles and the Relation of Gross Weights and Horsepowers of Commercial Vehicles. The third article Offtracking Calculations for Trailer Combinations, refers to some of the vehicle types shown.

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## NATIONAL BUREAU OF STANDARDS DEDICATION

Dedication ceremonies for new facilities of the National Bureau of Standards, Gaithersburg, Md., November 15 will be presided over by John T. Connor, Secretary of Commerce, and Dr. Allen V. Astin, Director, National Bureau of Standards. Dignitaries from Government, science, and industry also will participate in the ceremonies. To celebrate the construction and dedication of this new standards and testing complex, Secretary Connor is sponsoring an International Symposium of Technology and World Trade on November 16 and 17 at Gaithersburg.

The new $\$ 120$ million NBS laboratory complex consists of 15 major buildings constructed on a 565 -acre site. New laboratories and supporting facilities enable the Bureau of Standards to update its research programs in a rural environment removed from urban mechanical, electrical, and atmospheric disturbances. Expanded facilities include a nuclear research reactor and a linear electron accelerator for the establishment of measurements and standards. An Engineering Mechanics Laboratory was also added to the relocated facilities for work such as the calibration of rocket thrust measuring devices.

At the International Symposium of Technology and World Trade on November 16 and 17, experts from all over the world will examine and forecast the impact of technology upon the patterns and conduct of international trade and investment; consider the international environment needed for the wider generation and utilization of technology; and explore prospects for evolving policies and institutions that promote economic developemnt through technology and trade.

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# Braking Performance of Motor Vehides 

IY THE OFFICE OF<br>ISSEARCH AND DEVELOPMENT<br>REAU OF PUBLIC ROADS

Reported by ${ }^{1,2,3}$ SAMUEL C. TIGNOR,<br>Highway Research Engineer, Traffic Systems Division

## Introduction

ECAUSE IT is well known that adequate brake performance is necessary for the de operation of motor vehicles, the Bureau Public Roads in 1941 undertook a research pgram to determine at periodic intervals the buke performance levels of motor vehicles prating on the highway systems of the Lited States. Studies also were made in 119 and 1955. The most recent series of t ts was made beginning in July 1963 ; results 0 these tests are discussed in this article. Tle 1963 field testing was done as nearly as pssible in the same locations, in Maryland, Achigan, and California used for the 1949 ad 1955 tests. The information obtained f m this series of braking studies is expected $t$ be used to:

- Promote improvement in the general level obrake performance.

Since 1941, the Bureau of Public Roads periodically has conducted a research program to determine the braking performance levels of motor vehicles operating on public highways. The research results are used to promote improvement in the general level of brake performance for all types of vehicles, provide information that may be used in establishing highway design standards, and serve as a basis for revising brake performance standards. The most recent braking performance study, completed in November 1963, is discussed in this article.

- Serve as a basis for revising brake performance standards.
- Provide current motor-vehicle brake performance data that can be used to establish highway design standards, such as standards for stopping sight distance.
- Show the levels of brake performance for the different types of vehicles using the highways.


## Scope of Research

Tests to determine braking performance of motor vehicles operating on the highways were made on foreign, compact, and other (referred to here as standard size) passenger cars; single-unit trucks; and trailer combinations. Vehicles were selected at random from general highway traffic. All vehicles were stopped by a uniformed policeman; they were weighed; the weight and a descliption were recorded; and three emergency stops were

## EDITORIAL INTRODUCTION

In the three articles, Braking Perform[ace of Motor Vehicles, the Relation of coss Weights and Horsepowers of Comrorcial Vehicles, and Offtracking Calculatons for Trailer Combinations, printed in tis issue of the magazine, some common t:hnical terminology is used. For the cnvenience of the reader, these terms are eplained in the following paragraphs. Secific terms are defined in each article. Single-unit trucks and trailer combinatins have been designated by numerical ad letter combination codes based on the rumber of axles and their arrangement. The codes for these commercial vehicles are efined in the following list.

[^1]Presented at the October 1964 meeting of National Transptation, Powerplant, and Fuels and Lubricants Meeting, Che Society of Automotive Engineers, Inc., Baltimore, Md.
Bureau of Public Roads personnel who contributed to the Bureau of Public Roads personnel who contributed to the
scess of the research project include F. William Petring Scess of the research project include F. William Petring
(w with Ford Motor Coj.), Harry H. Hill. Harry Krashen, (w with Ford Motor Co.), Harry H. Hill, Harry Krashen,
Mliam H. Oliver, John M. Wright. James LoJacono, Hiliam H. Oliver, John M. Wright, James LoJacono,
F:hard C. Tennent, William J. Giacofei, Mrs. Madalene Fhard C. Tennent, William J. Giacofci, Mrs. Madalene
Endall (now retired), John F. Ly ons, and Mrs. Ruby Tice.
 Ipartment of State Highways, and the California Division olighways, and personnel from these State organizations asted in the field research. The Maryland Truck Patrol, t Sacramento Police Department, and the city of Sacraunto also contributed to the success of the project.

## 2-3 $\quad=2$-axle truck with 3 -axle trailer.

2 -S1-2 $=2$-axle truck-tractor with 1 -axle semitrailer and 2-axle trailer
2-S2-2 $=2$-axle truck-tractor with 2 -axle semitrailer and 2-axle trailer
2-S2-3=2-axle truck-tractor with 2 -axle semitrailer and 3 -axle trailer
3 -S1-2 $=3$-axle truck-tractor with 2 -axle semitrailer and 2-axle trailer
3 -S2-2 $=3$-axle truck-tractor with 2 -axle semitrailer and 2-axle trailer.
3 -S2-4 $=3$-axle truck-tractor with a 2 -axle semitrailer and 4 -axle full trailer. Also called a double trailer combination.
3 -S3-5 $=3$-axle truck-tractor with 3 -axle semitrailer and 5 -axle trailer.
Other technical terms used in the articles are defined in the following statements.

Gross vehicle weight.-Gross vehicle weight ( $\mathrm{G} V \mathrm{~W}$ ) is the empty weight, in pounds, including the weight of accessories and fuel, of a passenger car, truck, truck-tractorsemitrailer, or truck-tractor-semitrailer-full trailer combination, plus the weight of the cargo or payload carried at the time the vehicle was tested.
Brake system application and braking distance.-Brake system application and braking distance (BSABD) is the distance, in feet, traveled between the point at which the driver starts to move the braking controls and the point at which the passenger car or commercial vehicle is stopped.
Maximum deceleration.-Maximum deceleration is the peak deceleration measured in percent gravity (1 g.) that occurred during the stopping.
Pedal reserve.-Pedal reserve is the distance, in inches, between the floorboard or mat and the back of the pedal at the completion of a stop.
Brake system air pressure.-The brake system air pressure is air pressure, in pounds per square inch, indicated on the gage in the cab immediately after completion of a stop. This applies to vehicles equipped with some form of an airactuated brake system. Before any stops were made during this research, the air reservoir was filled by the air compressor.
Manufacturers maximum gross vehicle weight rating.-The manufacturers maximum gross vehicle weight rating is the
empty weight, in pounds, of the truck chassis and lubricants, water, fuel tank or tanks of fuel, plus the weight of cab, body, special chassis and body equipment, and the payload recommended by the chassis manufacturer.

Vehicle capacity.-Vehicle capacity for single-unit trucks is the same as the maximum gross vehicle weight rating; for trailer combinations it is the gross combination weight (GCW) recommended by the vehicle chassis manufacturer for a truck-tractor or truck used in combination with semitrailers or full trailers.

Mean.-The mean is a number that represents a set of numbers obtained by dividing the sum of all the numbers or elements in the set by the total number of elements in the set-expressed as: $\overline{\mathrm{X}}=\frac{\Sigma X}{N}$

Median.-The median refers to the middle number in a series of test data.

Mode.-The mode is the number in a set of data that occurs most frequently.
Standard deriation.-Standard deviation (S.D.) is the square root of the arithmetic mean of the squares of the deviations from the mean (1). ${ }^{4}$
Standard error of the mean.-Standard error of the mean is an estimate of the amount that an obtained mean may be expected to differ by chance from the true mean (2).
Gross horsepower.-The gross horsepower of a vehicle is the brake horsepower of the engine available at the clutch or its equivalent, when the engine is being operated but accessories such as fan, air compressor, generator, and muffler are not.
Net horsepower.-Net horsepower is the brake horsepower of the engine available at the clutch or its equivalent, when the engine is being operated with all the normal accessories. In other words, the net horsepower is the gross horsepower minus the horsepower absorbed by accessories such as fan, air compressor, generator, and muffler.

Weight-power ratio.-Weight-power ratio is the ratio of the gross weight of the vehicle or combination of vehicles to net horsepower of the powered unit. For example, if the gross weight of a trailer combination is 60,000 pounds and the net horsepower is 150 , the weight-power ratio is 400 pounds per horsepower.
${ }^{4}$ References indicated by italic numbers in parentheses are listed on page 82 .
made, each from a speed of 20 miles per hour (m.p.h.). Each driver was told that the tests were voluntary and that no punitive action would be taken regardless of the condition of the vehicles brakes. The braking performance was measured in terms of brake system application and braking distance the distance traveled between the point at which the driver starts to move the braking controls and the point at which the vehicle stopsand in terms of deceleration.

## Test sites

The tests were made at four locations: U.S. 40 near Elkton, Md., a 4 -lane divided highway; U.S. 24 near Erie, Mich., also a 4 -lane divided highway; U.S. 40 near Cordelia, Calif., an 8 -lane divided highway; and Elvas Ave., Sacramento, Calif., an undivided city street carrying crosstown traffic. In California, the Cordelia site was used to obtain the commercial vehicle sample, and the Elvas Ave. site was used to obtain the passenger car sample. At each of the other sites, both commercial vehicles and passenger cars were tested. Out-of-State vehicles were tested at each site.

The test section used at each study site was a dry, single-level through lane approximately a half-mile long, separated from other through lanes by rubber traffic cones and/or barricades. Signs were erected that instructed through drivers to merge to a lane other than the test lane and notified them that braking tests were being conducted. Scales were located next to the test lane and were used to determine the gross vehicle weight before the testing. The


Figure 1.-Trailing fifth-wheel, distancemeasuring device attached to a $2-\mathrm{S} 2$.


Figure 2.-Brake pedal switch for activating pavement marking and distance measuring devices.
scales at the sites in Michigan and Cordelia, Calif., were of the permanent pit type used by the States for enforcement of weight regulations. At the other test locations, portable scales were used.

Locked-wheel, passenger-car stops were made at each test section to determine the similarity of the coefficient of friction for the different test surfaces. The results of the locked-wheel stops showed that all of the surfaces had similar frictional characteristics, the average coefficient of sliding friction being 0.82 .

## Instrumentation

Instrumentation was primarily a test wheel, equipped with a distance measuring device and a portable decelerometer. The test wheel measured the speed of the test vehicle in miles per hour and the brake system application and braking distance in feet. The decelerometer measured the maximum deceleration occurring during the braking test in percent of 1 g . The instrumentation is shown in figures 1 through 4.

The test wheel (fig. 1), referred to as a fifth wheel, was equipped to start the distancemeasuring device when the driver touched his foot to a switch attached to the brake pedal (fig. 2). When the driver's foot first touched the brake pedal switch, an electrical circuit was completed and it was maintained by a holding relay until released by the observer. An observer, who rode with the test driver, recorded the distance shown on the dial of the distance recording device, the speed, the deceleration, and the other information relevant to the stop.

Speed of the test vehicle was measured in miles per hour by a voltmeter wired to a belt-driven generator, which was mounted on the frame of the test wheel (fig. 3). The observer held the voltmeter (fig. 4) and when a speed of $20 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. was reached, he told the driver to stop. A pendulum-type decelerometer (fig. 4) was used. A moving scale, indicating percent of 1 g ., was actuated by, and proportional to, the movement of a pendulum. When the test vehicle moved at a uniform speed, the pendulum assumed a vertical position; but when the speed was reduced by the application of brakes, the pendulum tended to move at the initial speed and thus swing forward. The tangent of the angle through which the pendulum moved from its vertical position was proportional to the deceleration. A scale reading of 80 percent thus would reflect a deceleration of $0.80 \times 32.2$, or 25.8 feet per second per second (ft./sec./sec.). The decelerations measured by a pendulum-type decelerometer are often larger than actual decelerations, which can be measured by more sophisticated equipment. The pendulum-type decelerometer, however, is effective for identifying vehicles that have improperly maintained brakes.
All equipment used for the braking performance tests was calibrated frequently during the tests to assure accuracy of test results. The speedometer or voltmeter was calibrated by measuring with the test wheel the time required to travel a measured mile at a constant speed. The accuracy of the
distance-measuring device was verified by us of an electric detonator mounted on th bumper. The detonator ejected a chal capsule that marked the pavement at th instant the driver touched his foot to th brake switch pedal-the same switch tha activated the distance measuring devic The brake system application and brakin distance shown on the dial for the test whe was compared with the distance measure between the chalk mark on the pavement an a point below the detonator on the test vehicl To calibrate the moving scale on the decele ometer, the instrument was placed on a know slope and the tangent of the slope compare with the scale reading. These periodic tes of equipment showed a variation of 2 percer or less between the test and theoretic results.

## Test procedures

When a vehicle was selected for testing, th driver was directed, by a uniformed office from the through lanes into an interview ar pit area adjacent to the test lane. The te procedures were explained to each driver ar those preferring not to participate in t] tests were permitted to continue.

On one of two cards, both having the san test number, the vehicle characteristics we recorded. The information noted includd vehicle type, make, model, year, type transmission, tire size, type of cargo, man facturers maximum gross vehicle weig rating, type of brake system, and number


Figure 3.-Dial on fifth wheel for measuri brake system application and braki distance.


Figure 4.-Placement of test instrumen tion.


Figure 5.-Passenger car weight distributions.
oraked axles; this card also had space for ording test data. On the other card, the ricle weight by individual axle was reded. The equipment for measuring the pike performance then was installed.
An observer seated next to the driver dited him to the test lane. Before any ts were conducted, the driver was told disengage the clutch during the stop and, it were a commercial vehicle, to set the hiting valve in the dry road position and to use the hand control valve during tests. Approximately three emergencye stops were made, each from a speed 20 m.p.h. Each stop was made upon observer's direction, when the test speed 1 been reached. The driver applied the bukes and maintained the vehicles maximum biking capacity. After each stop, the oserver recorded the brake system applicion and braking distance, the maximum
deceleration, and the pedal reserve or brake system air pressure.

As the test lane was separated from all through traffic by rubber cones, barricades, or both, an unobstructed lane was available for each test vehicle. Thus the $20 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. speed could be stabilized for the braking stops. To prevent interference from a vehicle inadvertently entering the test lane, a project vehicle-equipped with a flashing red light on top and a large sign mounted on the rear that stated DANGER-BRAKE TESTS-SUDDEN stop- followed the test vehicle. An observer also was in the project vehicle; he measured the lengths of any skid marks that were left by the test vehicle and entered these lengths on the weight data card. When the braking tests had been completed, the test equipment was removed from the vehicle and the driver was thanked for his cooperation. The equipment then was returned to the pit area for use on the next test vehicle.

## Analyses

In the analyses of test data, vehicles were classified according to vehicle type; capacity, based on manufacturers maximum vehicle weight ratings; test gross weights; and brake type. The braking performance results from the 1963 study were compared with the performance requirements of the Uniform Vehicle Code (5) and with the results of the previous studies. Statistical tests were performed at different points in the analyses to determine whether the difference in observed means was statistically significant and to obtain insight into the meaning of the results. Separate analyses were made for the passenger car and commercial vehicle test results; these analyses are presented separately. For both analyses, a 40 K 7010 IBM computer was used in different phases. The computer arranged the vehicles by State, vehicle type, brake type, manufacturers capacity weight rating groups, and test gross weight. In general, its use expedited the computation of statistics such as means, standard deviations, and confidence intervals.

## Passenger Cars

Passenger cars tested were classified as foreign, compact, and standard size. Because of the increase in popularity of the foreign and compact passenger cars and the frequency of their operation on the highways, an analysis of the braking performance of such vehicles was considered desirable. Also data for the foreign, compact, and standard size cars were combined and analyzed for comparison with the results of previous studies.

Any passenger car produced in a country outside the United States was placed in the foreign car category. Passenger cars not included in either the foreign or compact categories were classified as standard size cars. The criteria used to classify compact cars included primarily, the make of vehicle, year of production, gross weight, wheelbase, overall length, and horsepower, according to the method described by Cope and Liston (3). Automobile insurance company guides also were consulted.
The weight distributions for the foreign, compact, and standard size cars are shown in figure 5. Although some overlap of classi-

Tble 1.-Passenger cars tested and results of analyses of data by classification from 1963 braking study

| Data analyses | Foreign | Compact | Standard | Total |
| :---: | :---: | :---: | :---: | :---: |
| 3ross weight: |  |  |  |  |
|  | 2, 040 |  | 4,164 | 3,736 |
| S.D | 2,477 | 2,319 | ${ }^{4} 409$ | ${ }^{815}$ |
|  | 1,875 | 2,875 | 3,875 | 3,875 |
| Deceleration: |  |  |  |  |
| Number of cars ${ }^{1}$ - | 37 | 80 | 283 | 400 |
| Mean.......-...--feet/second/second | 28.6 | 29.7 | 29.3 | 29.3 |
|  | 2.73 | 2.45 | 2.76 | 2.70 |
|  | 30.6 | 32.2 | 32.2 | 32.2 |
| Distance: |  |  |  |  |
| Number of cars | 37 | 80 | 285 |  |
|  | 19.3 | 19.0 | 20.0 | 19.7 |
| S.D ${ }_{\text {Mode }}$ | 2.65 | 1. 16 | 2.09 | 2. 04 |
|  | 19 | 20 | 19 | 19 |

Number of cars shown does not always agree with number in weight and brake system a lication and braking distance columns as some of the ears did not have enough room foinstallation of the decelerometer.


Figure 6.-Passenger cars decelerations.


Figure 7.-Frequency distribution of brake system application and braking distances for passenger cars.
fications existed, it constituted less than 5 percent of the 402 passenger cars tested. To determine whether the passenger car classifications were significantly different, an analysis of variance was performed. The null hypothesis was formulated that no difference existed between the average test weight for the foreign, compact, and standard size passenger car classifications. A level of significance of 0.05 was used; in other words, about 5 chances in 100 existed that the hypothesis would be rejected when it should be accepted. The mean test weights were determined to have been unequal and sufficiently different to require individual analysis for each classification: each passenger car classification, the number of vehicles tested, the average or mean value, the standard deviation, and the mode for the gross vehicle test weight, deceleration, and brake system application and braking distance are listed in table 1.

## Braking Performance

Use of cumulative frequency distribution curves is a convenient method for comparing the relative performance of the different classifications of passenger cars. Frequency
distributions for deceleration and for brake system application and braking distances for each passenger car classification are shown in figures 6 and 7.
The frequency distribution for passenger car deceleration is shown in figure 6. In part B little change is shown to have occurred in the deceleration performance of all passenger cars since 1955 (4), however, in the 1963 tests nearly 16 percent more cars than in the 1955 study reached a peak deceleration of 1 g . The average deceleration for each passenger car classification was compared at the 0.05 level to determine whether the differences in means were statistically significant Only the foreign car comparison with the compact car showed significantly different decelerations.
The frequency distribution curve in figure 7 indicates the percentage of passenger cars capable of stopping in a given brake system application and braking distance from a speed of $20 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. In general the 1963 test results were better than those obtained in 1955, particularly above the 50th percentile level, as shown in part B. In part A of figure 7, data show a larger variability in the distances for the foreign cars than for the compact cars.

This difference in variability is also shor in table 1; the standard deviation of the bra system application and braking distance i the foreign car classification exceeds that f the compact car.
An analysis of the average of test data the brake system application and braking d tance for each passenger car classification w made and compared with the average for ea of the other classifications. The means the compact cars and standard size e: differed significantly at the 0.05 level. I analysis of the data for foreign cars compal with that for compact cars and of the dd for foreign cars compared with that for star ard size cars showed no significant differen at the 0.05 level; thus no real difference exist between the means of brake system appli tion and braking distance tests for these t passenger car classifications.

The braking performance of passenger e had improved since the first series of te were made in 1942 (5). The test data shot general reduction in the variability of brake system application and braking dista between 1942 and 1963; the results from 1963 tests had one-fifth the variability of 1942 results, although the 1942 results cluded data for some passenger cars equip with mechanical-type braking systems. general reduction in braking performance sults at the 85 th, 50 th, and 15 th percent are shown in figure 8 for the studies madi 1942, 1949, 1955, and 1963.

Of the passenger cars tested, only a fev the compact and foreign classifications vacuum power brakes, but 93 of the standard size passenger cars tested had ve um power brakes. The average brake sys application and braking distance for cars had vacuum power brakes was 20.1 feet c pared with 19.9 feet for cars that had reg hydraulic systems. Comparison at the level, showed no real or significant statist differences in the mean braking performa of the two systems.

## Uniform Vehicle Code

The National Committee on Unit Traffic Laws and Ordinances presently ret mends in its Uniform Vehicle Code (5) all passenger cars stop in 25 feet or less 1 a speed of $20 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. As computed, nearl percent of the passenger cars tested in stopped in 25 feet or less. At the 95 th pers ile level the passenger cars stopped in feet and at the 85 th percentile level passe cars stopped in approximately 22 feet. committee also recommends that all passe cars decelerate from a speed of $20 \mathrm{~m} . \mathrm{p}$. not less than $17 \mathrm{ft} . / \mathrm{sec} . / \mathrm{sec}$. As indicate the pendulum-type decelerometer the sme peak deceleration was 17.7 ft ./sec./sec. computed in the analysis, 95 percent of passenger cars could stop with a peak dece tion of more than $24.1 \mathrm{ft} . / \mathrm{sec} . / \mathrm{sec}$. 1 the results of the 1963 brake perform test, the Uniform Vehicle Code (5) seen be liberal. Perhaps the code requiren should be updated to encourage addit improvement in the overall braking perf ance of passenger cars.

## e of vehicle

In analysis was conducted on 285 standard passenger cars equipped with either sum power brakes or regular hydraulic kes to determine whether the average ke system application and braking disace varied with the age of the car. To ermine whether the brake system appliion and braking distances means were nificantly different, an analysis of variance s performed. The null hypothesis was mulated that no difference existed between mean braking distance regardless of the of the vehicle. A level of significance of 1 was used, and the mean brake system plication and braking distances for the ferent years were significantly different that level.
A linear regression equation that best fit e data was computed by the method of st squares. This linear regression is shown figure 9. The coefficients of correlation d the coefficients of determination were also cmputed. The coefficient of correlation ( $r$ ) a measure of the goodness of fit of the regession equation to the data; 1.00 indicates perfect fit and 0.00 indicates no fit ( 6 ). he coefficient of determination $\left(r^{2}\right)$, the suare of the coefficient of correlation, represnts the part of the total variance that can I: accounted for by the independent variable, fich here is the age of vehicle ( 6 ).
The coefficient of correlation of 0.28 indited that the regression curve did not fit the uta as well as it might have. The coefficient determination indicated that only 8 percent the total variation in the brake system pplication and braking distance can be tributed to the age of the passenger car. he remaining or unexplained variation must z attributed to other factors such as inadelate brake system maintenance and/or poor ake adjustment.
The fact that a large percentage of the ariability in brake system application and raking distance is unexplained, also is illusated in figure 9 . The 95 percent confidence iterval is shown in figure 9 by parallel lines .94 feet above and below the regression line $=0.149 x+19.44$. For example, if the brake ystem application and braking distance is to e estimated on the basis of age, for standard ze passenger cars 5 years old; the distance ould be expected to fall within the interval f 16.25 to 24.13 feet, 95 percent of the time. 'his large interval emphasizes that the age of passenger car is not by itself a good paramter for estimating braking performance.

## Sonfidence intervals

The classification of passenger cars, as (1) )reviously explained, represents samples of he passenger cars operating on the public lighways. In evaluating the braking per$d$ ormance of the entire population of cars dithin each classification, the means for each I sample classification were used to determine (1) he interval in which the population mean dr could be expected to fall with some degree of 1 zonfidence. The confidence interval selected fit was 95 percent; meaning if 100 samples were faken from the population, 95 of the sample


Figure 8.-Percentile levels of brake system application and braking distances for passenger cars.


Figure 9.-Mean brake system application and braking distances by age of passenger car.
means would be within the computed interval. In computing the confidence interval, the standard error of the mean was adjusted for a probability of 0.95 . The equation used for determining the confidence interval for the population mean was:
95 percent confidence interval $=$ sample
mean $\pm 1.96 \times$ standard error of the mean
The interval in which the population mean for gross weight, deceleration and the brake sys-
tem application and braking distance could be expected 95 percent of the time for the different classifications of passenger cars is shown in table 2.

## Commercial Vehicle Test Results

The commercial vehicles tested were grouped according to vehicle type, capacity group, and brake type. Results from tests made with similar or like vehicles could
then be considered together and the braking performance determined for the respective groupings. Types of commercial vehicles are shown in figure 10.

## Capacity Groups

All commercial vehicles were classified by capacity groups on the basis of the chassis manufacturers gross vehicle weight or gross combination weight rating as marked on the rating plate attached to the test vehicle. Single-unit trucks were classified as very light, light, medium, and heavy; trailer combinations were classified as light, medium, and heavy. The distribution of gross weight ratings by capacity groups is shown in table 3 . Sometimes the chassis manufacturers maximum gross weight for truck or truck-tractor used in combination with trailers was not available on the vehicles tested. These trailer combinations were classified as light, medium, or heavy on the basis of the power unit when it is used as a single-unit truck.

## Brake Types

Four types of braking systems are commonly used on single-unit vehicles: hydraulic, vacuum-booster hydraulic, air-booster hydraulic, or air-mechanical systems. On trailer combinations the power units are braked by vacuum-booster hydraulic, air-booster hydraulic, or air-mechanical systems. The semitrailers and full trailers within the trailer combination generally are braked by air-
mechanical or vacuum-mechanical systems. The brake types used on the vehicles tested are defined as:

Hydraulic ( $H$ ).-Hydraulic brakes have brake shoes that are actuated by hydraulicbrake cylinders operated with hydraulic-line pressure developed by a pedal-operated hydraulic brake master cylinder.

Vacuum-booster hydraulic (VBH).-Vacu-um-booster hydraulic brakes have brake shoes that are actuated by hydraulic brake wheel cylinders operated with hydraulic-line pressure developed by a vacuum-powered master cylinder or a vacuum-hydraulic power unit.

Air-booster hydraulic (ABH).-Air-booster hydraulic brakes have brake shoes that are actuated by hydraulic brake wheel cylinders operated with hydraulic-line pressure developed by an air-powered master cylinder or an air-hydraulic power unit.

Air mechanical (AM).-Air mechanical brakes have brake shoes that are actuated by a cam or wedge operated by an air-brake chamber through a mechanical linkage.

Vacuum-mechanical (VM).-Vacuummechanical brakes have brake shoes that are actuated by a cam or wedge operated by a vacuum-brake chamber through a mechanical linkage.

A code also was used to represent the system or systems employed in braking the vehicles. Each individual part of the code represents the braking system used in a single-unit truck


Figure 10.-Commercial vehicles.
or in one unit of a trailer combination. combination code consisting of two or th parts separated by hyphens indicates braking system used in each unit of the tra combination. For example, a truck-tract semitrailer, and full trailer combination hav a braking code of VBH-VM-VM would $h$ : vacuum-booster hydraulic brakes on the tru tractor and vacuum-mechanical brakes both the semitrailer and full trailer.

## Vehicle Sample Size

Approximately 300 commercial vehis were tested in each of the three States. each State the sample was composed of ner 50 percent single-unit vehicles and 50 perc combination vehicles. Test vehicles w chosen at each test site so as to obtail sample in which gross vehicle or gross ed bination weights were distributed as evenly possible from the lightest to heaviest weigl In table 4, the number of vehicles tested each State are shown by type, capacity gro and brake type. No truck-tractors $\pi$ semitrailers and full trailers were tested Maryland because none came along during testing period.

## Weight, Deceleration, and Distan Observations

Tables 5 and 6 show for each commer vehicle grouping the number of vehicles test the mean, the standard deviation, and minimum and maximum test results for gr vehicle weight, deceleration, and the br system application and braking distar Both tables present the results by vehicle $t$; and capacity group: table 5 shows the rest by type of brake system and table 6 by wei groups. For example, the mean brake systo application and braking distance for the hets capacity, 2 -axle, single-unit trucks bral by air-mechanical systems (AM) was 31.7 ff and the mean distance - without regard to type of brake system-for the heavy capac 2-axle, single-unit trucks having a gross veh weight between 10,000 and 20,000 pou was 29.7 feet.

The minimum and maximum results for gross weight, deceleration, and brak distance in the two tables should not specifically associated with each other. Tr results only indicate the spread of the $\delta$ for each individual parameter; they are extremes and define the low and high lim Minimum and maximum results for one rameter, such as deceleration, cannot be sociated with the corresponding results

Table 3.-Capacity group classifications commercial vehicles by manufactur ratings

| Capacity group | Manufacturers gross weight ratin |  |
| :---: | :---: | :---: |
|  | Single-unit trucks | Trailer combinations |
| Very light | Pounds 10,000 and less | Pounds |
| Medium. | 10,001-16,000-...- | 27,000 and less. |
| Heavy . | 24,000 and more. | 44,000 and mor |

able 1.-Classification of vehicles tested by type, capacity group, and brake type

| Commercial vehicles and I capacity group | Brake type | Number of vehicles tested in- |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Md. | Mich. | Calif. | Total |
| Single-unit trucks: 2-axle: |  |  |  |  |  |
|  | (H | 46 | 37 | 33 | 116 |
|  |  | 1 | $\frac{2}{7}$ | 3 | 3 14 |
| Light | VB11 | 17 | 26 | 21 | 64 |
|  |  | 2 | 4 |  | ${ }^{\text {fi }}$ |
| Medium... | VBH | 55 | 65 | $\stackrel{51}{2}$ | 171 4 |
|  | ABH | - | $\frac{2}{7}$ | $\stackrel{2}{2}$ | 4 10 |
|  | (VBH | 7 | 4 |  | 11 |
| Heavy - | AM. | 12 | 2 | 2 | 16 |
| 3-axle: Light. | VBH |  |  |  | 1 |
| Mediun | (VBH |  | 2 | 2 | 4 |
|  | AM | 1 | 1 | 1 | $\frac{2}{5}$ |
| Heavy | AM. | 11 | 6 | 14 | 31 |
| Truck-trae tors with semitrailers: 2-S1: |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  | ( $\mathrm{CBH} \mathrm{BH}-\mathrm{AM}$ - | 6 | 1 | 1 | 18 |
| Medium.... | AM-AM | 5 | 8 | 8 | 21 |
|  | ABH-VM | --. | 1 | ... | 1 |
|  | (VBH-VM. | 2 | 1 | -- | 3 |
|  | ABH-AM... | 3 |  |  | 3 |
|  | $\left\lvert\, \begin{aligned} & \text { AM-AM } \\ & \text { AM-VM }\end{aligned}\right.$ | 15 1 | 15 | $\stackrel{29}{1}$ | $\stackrel{5}{2}$ |
| 2-S2: |  |  |  |  |  |
| Medium... | $\left\{\begin{array}{l} \mathrm{YBH}-\mathrm{VM} \\ \mathrm{ABH}-\mathrm{AM} \end{array}\right.$ |  | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ | 3 | 1 |
| меdим | AM-AM..-- | 7 |  |  | 13 |
| Heavy | $\left\{\begin{array}{l}\text { ABH-AM } \\ \text { AM-AM }\end{array}\right.$ | 104 | 1 | 10 | - |
|  |  |  |  |  |  |
| $\begin{aligned} & \text { 2-83: } \\ & \begin{array}{l} \text { Medium..... } \\ \text { IIeavy } \end{array} . . \text {.-. } \end{aligned}$ | AM-AM |  | 1 |  | 1 |
|  | AM-AM. | ---- | 1 | ---- | 1 |
| $3-82$ : |  |  |  |  |  |
| Medium | AM-AM | -.. |  |  | 1 |
| Heavy - | $\left\{\begin{array}{l} A B H-A M \\ A M-A M \end{array}\right.$ | 22 | 15 | 31 | ${ }_{98}^{1}$ |
| Trucks with full trailers: 2-2: Heavy...-3-2: Heavy $\qquad$ |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  | AM-AM. | --- | 2 | ---- | 2 |
|  | AM-AM. | - | 1 | 25 | 26 |
| Truck-tractors with semitrailers and full trailers: 2-51-2: Medium |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  | VBHII-VM- | --- | --- | 1 | 1 |
| Heavy | VM-AM- | --- | 8 | 40 | 48 |
| 2-52-2: <br> Medium.... <br> Heary $\qquad$ | AM-AM- | -- | 1. |  | 1 |
|  | AM. |  |  |  |  |
|  | AM-AM- | --- | 4 | -- | 4 |
| $\begin{gathered} \text { 2-S2-3: } \\ \text { Heavy } \end{gathered}$ |  |  |  |  |  |
|  | AM-AM- |  | 4 |  | 4 |
| 3 S1-2:Heavy _ |  |  |  |  |  |
|  | AM-AM- |  |  | 1 | 1 |
| 3-S2-2:Heavy |  |  |  |  |  |
|  | AM-AM- |  | 2 |  | 2 |
| 3-\$3-5: |  |  |  |  |  |
|  | $A M-A M-$ | --- | 2 |  | 2 |
| Other combinations: |  |  |  |  |  |
|  |  |  |  |  |  |
| Truck drive-awaytowaway |  |  |  |  |  |
| Heavy | (VBH |  | 1 |  | 1 |
|  | AM. | --- | 1 |  | 1 |
| $\begin{gathered} \text { Housetrailer } \\ \text { factory } \\ \text { tediaway: } \\ \text { Medium.... } \end{gathered}$ |  |  |  |  |  |
|  | VBH-E.- | 2 | 1 | 1 | 4 |
| Single-unit trucks with unbraked utility trailer: Medium |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  | VBH |  | 3 |  | 3 |
|  |  | 324 | 357 | 280 | 961 |



Figure 11.-Cumulative frequency distributions of minimum brake system application and braking distances and decelerations.



Figure 12.-Percentile levels of brake system application and braking distances for vehicles by year.

Talule 5. - Analysis results for gross vehicle weight, braking system application and braking distance, and deceleration, by type of bra system


[^2]Le other two. For example, in the elassication under truck-tractors with semitrailers id full trailers and for all other than 2-S1-2, he heary capacity group, maximum deceleraon of 32.2 feet per second should not be sociated with the maximum gross weight of $32,57(1)$ pounds. It would be more approiate to associate the maximum deceleration vehicles in this classification with the inimum weight and the minimum deceleraon with the maximum weight. However, ie fact that the distance required to stop creases with an increase in gross weight ust be considered.
All vehicles tested did not have decelerations 32.2 feet per second per second, or 1 g . he deceleration results shown in the tables e sometimes higher than the actual decelations that would be measured by more phisticated equipment. Some, but not all, the vehicles within the different classications had indicated maximum decelerations : 1 g .; the particularly heavily loaded vehicles ad decelerations less than 1 g . The pen-lum-type decelerometer used often inicated decelerations of 1 g . when the vehicle . Juncerl, hopped, or jumped during brake pplication. This was particularly evident hen the vehicles tested were carrying relively light loads in comparison to design rads. The test results do show the relative celeration performance relations between ie different vehicle classifications.

## traking Performance by Vehicle Type

The differences in braking performance Itributed to different types of vehicles are lown by the frequency distribution curves i figure 11 for the brake system application nd braking distances and deceleration. The urves show the braking performance in arcent of vehicles tested by vehicle type, hich stopped in a given distance or less, which reached a deceleration of a given or rger value when simulating an emergency op from 20 m.p.h. The decelerations reasured were not sustained throughout the ops but were the maximum decelerations -corded during the stops. The brake system pplication and braking distance and the aceleration frequency distributions are exience that the smaller vehicles are capable i beiter braking performance.
The improvement in braking performance : $)$ different types of commercial vehicles om $1!142$ to 1963 is shown in figure 12 by le 15 th, 50 th, and 85 th percentile levels (4). a general, braking performance has improved uring the years in a reduction in the distance quired to stop and a decrease in the raribility of brake system application and raking distance. This trend in continuig improvement in braking performance was vident in the results of the 1963 brake tests. The relative effect that different capacity roups and weight groups have on the braking erformance of vehicle types is shown by the ata in figure 13. The average brake system pplication and braking distance for each articular grouping was computed and is hown in the figure as a bar of a length in roportion to the respective distance. In


Figure 13.-Braking performance by vehicle types, capacity groups, and weight groups.
normal highway operation, brake system application and braking distance increases with weight for a given type of vehicle and this fact is confirmed by the test data shown (fig. 13).

## Braking Performance in 1955 and 1963

The average weight and the average brake system application and braking distance is given in table 7 by type of wehicle for the: rehicles studied in 1955 and 1963 . For some types the average weight varied little from 195.5 results, but the average weight for others varied considerably (4). Part of the variation in average weight can be explained by the chance selection of vehicles to be tested. However, part of the rariation in weight also can be attributed to operators of commercial whicles changing from use of one type of vehicle to another for economic reasons. For example, the $2-S 1$ vehicles currently are being used to carry lighter loards than previously, although no reduction has been made in the permissible legal weight limits.

The National Committee on Cnifrom Traffic Laws and Ordinances specified, in Uniform Vehicle Code (5), the minimum decederation and maximum brake system application and braking distanees that motor vehicles operating on the highways shou'd obtain when simulating emergener stop) from 20. m.p.h. A large percentage of vehicles in the 1963 study met the code requirements; these data are given in table 8 . The vehicle types that did not meet the braking requirements of the code were the truck-full trailer and the truck-tractor-semitrailer-full trailer combinations. However, when the brales on these large vehicle combinations are adjusted properly, they can meet the codr requirements. For example, two $3-8,3-5$ trailer combinations, weighing approximately 133,000 pounds each, were tested. The two trucktactors were the same make, model, and year, and an air-mechanical brake system was used in each. One trailer combination stopped in 69 feet from 20 m .p. h. and the other stopperd in 45 feect, i2 feret less thath the corle requirement. No maintenanee had been

Table 6．－Analysis results for gross vehicle weight，braking system application and braking distance，and deceleration by gross vehich weight group

performed on cither trater combination in preparation for the tests．It is almost certatin that the drailer combination that stopped in 69 feet could have stopped in a considerably shorter distance if its brakes had been adjusted immerliately before the test．It is also pos－ sible that a brake adjustment could have im－ proved the braking performance of the other trater combination．

## Arle Londs

Not all rehicle types could be considered in the analyses because wither too few vehieless of a given type were tested or weights carried on the principal load－carrying axles varied execssively：Axle loads could be analyzed for only the 2，2－S1，2－N゙2，and ：3－S2 types of vehicles．The results from the analyses of the test data for $2,2-51$ ，and $3-52$ vehicles were compared with the test results for similar rehicles from previous studies（4）． Because of large variations in the weights carried on the principal load－carrying axles，
previous 2－S2 test results could not be com－ pared with the 1963 study results．

The performance of 2 and $2-S 1$ vehicles from the brake research studies of 1949， 1955 ，and 1963 are shown in figure 14 ．In general，the braking performance of these two types of vehicles improved from one study to the next．The weights on the steering axles were not considered in the data shown．For the type 2 ，single－unit vehicles，the rear axles were grouped in weight increments of 4,000 pounds and the braking performance wats then computed for the groups and plotted at the mirlpoint of the weight group．The same analysis procedure was used for the 2－S1 vehicles，however，data were considered only for those trailer combinations for which the weights of the truck－tractor drive axle and the trailer axle were in the same 4,000 －pound group．

Primarily because of difficulty encountered in establishing weight inerements in which a
sufficient number of observations could obtained for $2-52$ of trailer combinations， data were treated differently．The method least squares was used to compute the lin regression equation that best fit the cata． the analysis of the data for $2-52$ trailer co binations information was used only on traj combinations for which the truck－trac drive axle weight equaled or exereeded 16,1 pounds．In the analysis of the datal on 3－S2 combinations，test results were used o for trailer combinations in which both sets tandem axles were within 4,000 pounds of e ： other．

The braking performance for the 2－ボ2 ： 3－S2 trailer combinations in relation to weight on the tandem axles is shown in fig 15．The regression curve determined for $2-82$ trailer combinations is approximat parallel to and 2 feet below the curve for 3－S2 trailer combinations．The coofficient
able 6.-Analysis results for gross vehicle weight, braking system application and braking distance, and deceleration by aross vehicle weight group-Continued

errelation for the $2-\mathrm{S} 2$ and $3-\mathrm{S} 2$ trailer combations of 0.41 and 0.60 , respectively, indates that the regression curves did not fit it data as well as might be hoped for. A lige amount of scatter about the regression Lle, caused by a large variation in the brake sstem application and braking distance, was riponsible for the small coefficients. The 1. cefficients of determination indicate that 17 rad 36 percent of the total variation in brake stem application and braking distance for te $2-\mathrm{S} 2$ and $3-\mathrm{S} 2$ trailer combinations, re"sectively, can be attributed to the tandem ale weights and the remaining or unexplained I riation must be attributed to other factors. iis ch factors include inadequate brake system (saintenance and/or poor brake adjustment. ne linear regression curve for the $3-\$ 2$ thiler combinations tested in 1955 is also sown in figure 15 . This curve indicates tat the braking performance in relation to Indem axle loadings was poorer in the 1955 $\therefore$ sidy than in the 1963 study. A larger per"' cntage of the variation in brake system ap"I eation and braking distance in the 1955 iridy could be explained by tandem-axle invight.
fol Before the braking performance in relation the manufacturers gross vehicle or com-

Table 7.-Average weight and brake system application and braking distance for commercial vehicles tested in 1955 and 1963

bination wcight rating could be evaluated, the manufacturers weight rating for the test vehicle had to be determined. The manufacturers gross vehicle weight ratings were used to evilluate the braking performanee
of single-unit trucks and the manufacturers gross combination weight ratings were used to evaluate braking performance of trailer combinations. Usually the weight rating appears on the manufacturers identification

Table 8．－Braking test results for 1955 and 1963 compared with Uniform Vehicle Code requirements

| Commercial vehicles | Deceleration |  |  | BSABD |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | UVC re－ quirements | Vehicles within requirements |  | UVC re－ quire－ ments | Vehicles within requirements |  |
|  |  | 1955 | 1963 |  | 1955 | 1963 |
| Single－unit trucks： <br> 2－axle，very light． <br> 2－axle，other than very light $\qquad$ <br> 3 －axle | $\begin{gathered} \text { Ft./sec./sec. } \\ 14 \\ 14 \\ 14 \end{gathered}$ | $\begin{gathered} \text { Percent } \\ 100 \\ 94 \\ 85 \end{gathered}$ | Percent 100 98 91 | $\begin{aligned} & \text { Feet } \\ & 30 \\ & 40 \\ & 40 \end{aligned}$ | $\begin{gathered} \text { Percent } \\ 84 \\ 84 \\ 53 \end{gathered}$ | $\begin{gathered} \text { Percent } \\ 97 \\ 95 \\ 75 \end{gathered}$ |
| Truck－tractors with semitrailers： $\begin{aligned} & 2-81 \\ & 3-2 \\ & 3 \end{aligned}$ | $\begin{aligned} & 14 \\ & 14 \\ & 14 \end{aligned}$ | $\begin{aligned} & 83 \\ & 82 \\ & 76 \end{aligned}$ | $\begin{aligned} & 97 \\ & 91 \\ & 89 \end{aligned}$ | $\begin{aligned} & 50 \\ & 50 \\ & 50 \end{aligned}$ | $\begin{aligned} & 81 \\ & 80 \\ & 64 \end{aligned}$ | $\begin{aligned} & 97 \\ & 94 \\ & 92 \end{aligned}$ |
| Trucks with full trailers Truck－tractors with stinitrailers and full trailers | $\begin{aligned} & 14 \\ & 14 \end{aligned}$ | $\begin{aligned} & 51 \\ & 69 \end{aligned}$ | $\begin{aligned} & 80 \\ & 79 \end{aligned}$ | $\begin{aligned} & 50 \\ & 50 \end{aligned}$ | $\begin{aligned} & 38 \\ & 41 \end{aligned}$ | $86$ |

Table 9．－Mean，standard deviation，and minimum ratios of GVW to manufacturers weight rating

| （＇ommercial vehicles（all capacity groups） | Gross vehicle weight， 1，000 lbs． | Number | Ratio， | gross velicle weight |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | manufacturers weight rating |  |  |
|  |  |  | Mean | standard deviation | Minimum | Maximum |
| Single－unit trucks： |  |  |  |  |  |  |
|  | $0-9.9$ $10-19.9$ | 217 161 | 0.65 0.71 | 0.192 0.196 | 0.37 0.37 | 1． 12 1.26 |
| 2－axie | 20－29．9 | 36 | 1.11 | 0． 208 | 0． 65 | 1． 49 |
|  | 30－39．9 | 1 | 1.05 | －－－－－－－ | 1． 05 | 1.05 |
|  | 10－19．9 | 20 | 0.52 | 0． 146 | 0.36 | 0.92 |
| 3－axde． | $20-29.9$ | 15 | 0．73 | 0.316 | 0.45 | 1． 59 |
|  | $30-39.9$ $40-49.9$ | 3 4 | 1． 19 1.15 | －－－－－－－－－ | 0.93 1.06 | 1.63 1.36 |
| Truck－t ractors with semitrailers： |  |  |  |  |  |  |
| $2-$ S 1 | 10－19．9 | 35 | 0． 40 | 0． 067 | 0． 31 | 0.56 |
|  | $20-29.9$ | 45 | 0.51 | 0.161 | 0． 27 | 0.81 |
|  | 30－39 9 | 16 | 0.71 | 0.128 | 0． 48 | 1． 00 |
| 2－s2 |  |  |  |  |  |  |
|  | 10－19．9 | 6 | 0． 43 |  | 0． 34 | 0． 64 |
|  | 20－29．9 | 62 | 0． 47 | 0． 130 | 0． 30 | 0.97 |
|  | $30-39.9$ $40-49.9$ | 34 | 0.67 0.81 | 0． 105 | 0.46 0.53 | 0．87 |
|  | 50． 59.9 | 58 | 1． 02 | 0.158 | 0． 70 | 1． 41 |
|  | 60.69 .9 | 2 | 1．25 | －．．．－－－ | 1． 08 | 1． 41 |
| $3-8$. | 20－29 9 | 22 | 0． 42 | 0.055 | 0.31 | 0.54 |
|  | 30－39．9 | 14 | 0． 51 | 0．0ti3 | 0.43 | 0.61 |
|  | 40－49．9 | 4 | 0． 68 |  | 0.58 | 0.84 |
|  | 50－59．9 | 11 | 0.81 | 0．084 | 0.69 | 0.93 |
|  | 60－69．9 | 17 | 0.94 | 0.114 | 0． 80 | 1.15 |
|  | $70-799$ $80-89.9$ | 13 1 | 1.09 1.24 | 0.164 | 0.90 1.24 | 1.45 1.24 |
|  |  |  |  |  |  |  |

Table 10．－Braking performance of trailer combinations with and without brakes on the steering axle

| Commercial vehicles | Brakes on steering axle |  |  |  | No brakes on steering axle |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Vehicles tested | A verage weight | Average decelera－ tion | Average BSABI） | Vehicles tested | Average weight | Average decelera－ tion | Average BS」BI） |
| Truck－tractors with semi－ trailers： $3 \therefore$ | No． fio | $\begin{gathered} L / 心 . \\ 49.800 \end{gathered}$ | Ft．／sec．／ sec． 23 | Ft 37 | N゙o． 40 | $\begin{aligned} & L b s . \\ & 51,000 \end{aligned}$ | Ft．／sec．／ sec． 21 | F\％ 40 |
| ```Truck-tractors with semi- trailurs atd full trailers: 2-S1-2 3N2``` | $\stackrel{24}{1}$ | $\begin{aligned} & 56400 \\ & 39.000 \end{aligned}$ | $\begin{aligned} & 18 \\ & 3: 3 \end{aligned}$ | $\begin{aligned} & 46 \\ & 35 \end{aligned}$ | $\begin{array}{r} 21 \\ 1 \end{array}$ | $\begin{aligned} & 64.400 \\ & 35.000 \end{aligned}$ | $\begin{aligned} & 19 \\ & 27 \end{aligned}$ | $\begin{aligned} & 48 \\ & 39 \end{aligned}$ |

plate attached to the rehicle：howerer，of en the manufacturers specifications had to be consulted．When the weight rating had been determined，a ratio was computed be－ tween the groses whiele weight and the math－ ufacturers weright rating for test vehicles． Sometimes the ratio could not be computed becaluse the manufacturers weight rating could not be found on the wehiele or deter－ mined from the rehicle specefications；data for these vehieles were not used in the analysis．

The amalysis of braking performanee ratio by GVW and manufacturers weight rating was made for the 2－and 3 －axle，single－unit trucks and for the $2-8,2-\infty 2$ ，and $3-2$ truck－tractor－semitrailer combinations．Bc－ c：ase the manufacturers gross combination weight rating for many of the multicom－ bination vehicles could not be determined， data for these rehickes were not included in the amalysis．Results of the analysis of braking performance in relation to the ratio

Table 11．－Braking performance with al axles braked and without steering axle braked，in test by Committee on Winte Driving Hazards

| Commercial vehicles | Weight | BSABI）from 20 m．p．h． |  |
| :---: | :---: | :---: | :---: |
|  |  | All axles braked | Steering axles not braked |
| $\begin{aligned} & 3-\mathrm{S} 2 \\ & 3-2 \\ & 2-\mathrm{S} 1-2 \end{aligned}$ | Pounds <br> 24， 830 <br> 22， 300 <br> 22， 090 | $\begin{gathered} \text { Feet } \\ 24 \\ 21 \\ 26 \end{gathered}$ | $\begin{gathered} \text { Feet } \\ 30 \\ 25 \\ 31 \end{gathered}$ |

of gross weight and manufacturers weigh ratings are shown in table 9 by vehicle typ and weight group．

The effect of an increase in the gross weigh to the manufacturers weight rating on brakin performance is shown in figure 16 ．As th ratio of the gross vehicle weight to mas ufacturers weight rating increased，the brak system application and braking distane also increased but the peak deceleratio decreased．Mean values for ratio，decelera tion，and distance are plotted in figure 1 at the mean weight for the different tes weight groups．All trailer combinations except the $2-S 1$ ，had gross vehicle weigh1 of more than the recommended manufacture rating；this is indicated by a ratio of mol than 1 ．With one exception，when the rati was less than 1，the vehicles met the Unifor Vehicle Code（5）recommendations for brakir performance：the 3 －axle，single－unit truck required approximately 2 feet more than th recommended distance of 40 feet from speed of $20 \mathrm{~m} . \mathrm{p} . \mathrm{h}$ ．In an evaluation of th braking performance of the types of comme cial vehicles tested in this researeh，the fat must be recognized that braking systen can be designed to meet given performant requirements provided that the gross vehic weight does not exeeed the manufacture suggested weight rating and that the brakil systems are properly maintained．

## No Brakes on Steering Axle

Some States and the Interstate Commer Commission permit，in their motor－vehis regulations，certain vehicles to operate wit out any brakes on the steering axle．In t 1963 braking performance test，combinati vehicles were tested that did not have fro wheel brakes；these are listed in table 1 Except for the 3－s2 trailer combinations large difference existed in the mean gre weights between the trailer combinatio that did and those that did not have brak on the steering axle．Consequently，$t$ longer distance requied for stopping by $t$ combinations without front wheel brak eamot be attributed entirely to the fact th one axte was not braked the poorer pi formance also could have been attribut partially to the weight differential．T additional distance was approximately 2 to： feet．

In 1955 the National Sufety Comei Committee on Winter Driving Hazards ec ducted tests on dry pawement for emp combination vehicles，both with and withe
te steering axles braked (6). The fundings terms of the brake system application Id braking distance when making emergeneype stops from $20 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. for both braking mditions are shown in table 11 . The brake stem application and braking distance creased 4 t.o 6 feet, when the stecring axle as not braked.

## Confidence Intervals

The commerial vehicles tested were rouped according to type, capacity, brake sterm, and weight. Similar commercial ehicles were classified into groups, and then onsic(red as samples from the group populaons. The standard errors of the means ere computed for the groups that had at ast 10 observations. Confidence intervals ren were computed for each commereial chicle group having 10 or more observations. iy using the confidence interval, the levels of raking performance for each individual roup could be estimated and the degree of liability of estimates known. For each roup, the 95 percent confidence intervals for he means of the gross weight, deceleration, nd brake system application and braking istance were determined; their confidence itervals were computed in the same manner s those for the passenger cars. The confience intervals by type of brake systems and y weight group are shown in table 12 .

## Findings of Analyses

## assenger cars

The following findings concerning passenger ars were obtained from analyses of the 1963 lest data.

- The average weights of foreign cars, ompact cars, and standard size cars differed ignificantly from each other at the 0.05 level.
- Little change has occurred since 1955 in he deceleration performance of all passenger "ars, when considered as a group. Comparion of decelerations of the foreign cars with the compact ears, however, showed that the - ompact cars had significantly larger average lecelerations in the 1963 tests at the 0.05 evel.
- Some decrease since 1955 in the brake ystem application and braking distance was hown in the 1963 test results, particularly ibove the 50th percentile level. In the comJarison of the average brake system applicaion and braking distances for the different passenger car classifications studied in 1963, mly results of the compact car comparison with the standard size car differed signifisantly at the 0.05 level.
- The variability in the brake system application and braking distances has continued to decrease since 1955 .
- The mean brake system application and braking distances for the different test years Frere significantly different at the 0.01 level.
- According to 1963 test results, 95 percent 1 of the time the mean brake system application and braking distances for the passenger car slassifications can be expected to be within the following distance intervals: foreign, " 18.4 to 20.2 feet; compact, 18.7 to 19.3 fcet; and standard size, 19.8 to 20.2 feet.


Figure 14.-Brake systom application and braking distances by vehicle asle weights, by test years.


Figure 15.-Brake system application and braking distances by tandem axle weights for 2-S2 and 3-S2 vehicles.

## Commercial vehicles

The following findings were obtained from the analyses of the 1963 test results for commercial vehicles.

- The average brake system application and braking distance since 1955 has decreased 2 to 3 feet for the very light 2-axle trucks to 10 feet or more for some of the heavier trailer combinations. Since the 1955 tests all the commercial vehicles had improved deceleration performance from approximately 5 percent for very light 2-axle trucks to 15 pereent for heavier multitrailer combinations.
- The variability in the brake system application and braking distance for similar types of vehicles continued to decrease.
- The brake system application and braking distance generally has decreased since 1955 regardless of the vehicle type, weight group, or manufacturers capacity group.
- In the 1963 tests, a larger percentage than in the 1955 tests of commercial vehicles could meet the brake system application and braking distance and deceleration requirements recommended in the Uniform Vehicle Code.


Figure 16.-Relation of GVW to manufacturers weight rating, distance, deceleration, and weight.

- Results of the axle load analysis showed that the brake system application and braking distances for similar axle loadings decreased approximately 3 feet from 1955 to 1963 for both 2-axle, single-unit trucks and 2-S1 trailer combinations.
- The relation between the distance required to stop and tandem axle weights of 2S2 and 3-S2 trailer combinations could not be clearly defined in the analysis of test results. Only a small part of the total variation in the brake system application and braking distance could be explained by axle loading.
- When the ratio of gross vehicle weight to the manufacturers weight rating was less than 1, the rehicles met the Uniform Vehicle Code recommendations. However, the 3 -axle, single-unit trucks required approximately 42 feet rather than the 40 feet to stop at $20 \mathrm{~m} . \mathrm{p} . \mathrm{h}$.
- The 1963 test results and the National Safety Council Committee on Winter Driving

Hazards studies showed that the brake system application and braking distance is several feet longer when the steering axle is not braked than when it is.

- According to the 1963 test results, the mean brake system application and braking distance for all commercial vehicles of a given type can be expected 95 percent of the time to be within the following distance intervals: $2-$ axle, single-unit trucks, 26 to 27 feet; 3-axle, single-unit trucks, 31 to 37 fcet; 2-S1, 31 to 34 feet; 2-S2, 35 to 37 feet; $3-$ S2, 36 to 40 feet; 3-2, 38 to 45 feet; and $2-\mathrm{S} 1-2,43$ to 50 fect.


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Table 12.-Confidence interval for commercial vehicles according to brake system and gross vehicle weight groups

| Commercial <br> vehicles and capacity groups | Brakesystems | Standard error of mean |  |  | 95 percent confidence intervals |  |  |  |  |  | Gross vehicle weightgroups | Standard error of mean |  |  | 95 percont confidence intervals |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Gross weight | $\begin{aligned} & \text { De- } \\ & \text { celer- } \\ & \text { ation } \end{aligned}$ | BSABD | Gross weight |  | Deceleration |  | BSABD |  |  | Gross weight | De-celeration ${ }^{2}$ | BSABD | Gross weight |  | Deceleration 2 |  | BSABD |  |
|  |  |  |  |  | From | To | From | To | From | To |  |  |  |  | From | To | From | To | From: | To |
| Single-unit trucks: 2-axle: | $\left\{\begin{array}{l} \text { Types } \\ \text { All......... } \end{array}\right.$ | $\begin{gathered} \text { Pounds } \\ 103.1 \end{gathered}$ | Ft.l sec./ sec. 0.35 <br> 0.35 | $\begin{aligned} & \text { Feet } \\ & 0.34 \end{aligned}$ | $\left\|\begin{array}{c} \text { Pounds } \\ 4,480 \\ \hdashline 4.540 \end{array}\right\|$ | $\begin{gathered} \text { Pounds } \\ 4,890 \end{gathered}$ | Ft. 1 <br> sec. $/$ <br> sec. <br> 26.9 <br> 27.0 | Ft. 1 <br> sec. 1 <br> sec. <br> 28.3 <br> 28.4 | $\begin{aligned} & \text { Feet } \\ & 20.9 \end{aligned}$ | $\begin{aligned} & \text { Feet } \\ & 22.3 \end{aligned}$ | $\begin{aligned} & 1,000 \\ & l, 0.4 \\ & 0-4.9 \\ & 5-9.9 \end{aligned}$ | $\begin{gathered} \text { Pounds } \\ 54.0 \\ 146.5 \end{gathered}$ | Ft. 1 sec. $/$ sec. 0. 4.5 0. 54 | $\begin{aligned} & \text { Feet } \\ & 0.45 \\ & 0.48 \end{aligned}$ | $\begin{gathered} \text { Pounds } \\ 3,950 \\ 5,630 \end{gathered}$ | $\begin{gathered} \text { Pounds } \\ 4,160 \\ 6,200 \end{gathered}$ | Ft. 1 sec. sec. <br> 27.0 <br> 26.2 | Ft. 1 sec. $/$ sec. 2x. 8 28.4 | $\begin{aligned} & \text { Feet } \\ & 20.4 \\ & 21.5 \end{aligned}$ | $\begin{aligned} & \text { Feet } \\ & 22.2 \\ & 23.3 \end{aligned}$ |
| Light..........- | $\begin{aligned} & \text { All } \\ & \left\{\begin{array}{l} H \\ \text { VBH } \\ \text { Al } \end{array}\right. \end{aligned}$ | 115.4 $1,113.4$ 558.3 497.4 20.4 | 0. 35 1. 38 0.72 0.67 0. | 0.33 1.95 0.93 0.73 0.70 | 4,540 7.940 9.570 9.600 | 4. 990 12. 310 11. 70 11, 550 | 27.0 19.2 25.1 24.4 | $\begin{aligned} & 28.4 \\ & 24.6 \\ & 27.9 \\ & 27.0 \end{aligned}$ | $\begin{aligned} & 21.0 \\ & 25.6 \\ & 25.0 \\ & 25.6 \end{aligned}$ | $\begin{aligned} & 23.2 \\ & 33.2 \\ & 27.8 \\ & 28.4 \end{aligned}$ | $\left\{\begin{array}{l} 0-9.9 \\ 10-19.9 \end{array}\right.$ | $\begin{aligned} & 168.6 \\ & 621.4 \end{aligned}$ | $\begin{aligned} & 0.71 \\ & 1.21 \end{aligned}$ | $\begin{aligned} & 0.54 \\ & \text { 1. } 22 \end{aligned}$ | $\begin{array}{r} 7,620 \\ 12,820 \end{array}$ | $\begin{array}{r} 8,280 \\ 15,250 \end{array}$ | $\begin{aligned} & 26.2 \\ & -26.0 \\ & 21.3 \end{aligned}$ | $\begin{array}{r} 28.4 \\ \begin{array}{r} 28.8 \\ 26.1 \end{array} \end{array}$ | $\begin{array}{\|l\|} 21.5 \\ 23.4 \\ 27.8 \end{array}$ | $\begin{gathered} 23.3 \\ -25.6 \\ 32.6 \end{gathered}$ |
|  | VBH | 367.7 2, 019.6 | 0. 38 2. 38 | 0.42 5.32 | 12,910 13,590 | 14,350 21,500 | 24.8 14 | 26.2 23.5 | 26.6 27.6 | 28.2 48.2 | $\left\{\begin{array}{c} 0-9.9 \\ 10-19.9 \end{array}\right.$ | $\begin{array}{r} 97.9 \\ 265.7 \end{array}$ | $\begin{aligned} & 0.58 \\ & 0.45 \end{aligned}$ | 0.64 0.59 | $\begin{array}{r} 8.540 \\ 13,260 \end{array}$ | 8,920 14,300 | 26.9 24.4 | 29. 26 | 23.3 26.9 | 25.8 29.3 |
| Heavy | All | 354.0 | 0.38 | 0. 50 | 13. 070 | 14, 460 | 24.4 | 25.8 | 27.1 | 29.1 | 20-29.9 | 441.7 | 0.92 | 1. 50 | 21, 970 | 23,700 | 17.4 | 21.0 | 32. 4 | 38.2 |
|  | $\left\{\begin{array}{l}\text { VBH } \\ \text { AM }\end{array}\right.$ | $1,594.0$ $1,312.3$ 1.014 .6 | 1.42 0.91 0.96 | 1. 74 | 12,650 15,360 | 18,900 20,500 | 24.8 20.2 2. | 30.4 23.8 26.8 | 27.0 29.1 | 33.8 34.3 3.3 | 10-19.9 | 535.6 | 0.98 | 0.85 | 13,720 | 15,820 | 23.2 | 27.0 | 28.0 | 31.4 |
| All capacity groups.- | All | 1.014 .6 237.2 | 0.96 0.37 | 1. 06 0.42 | 15,070 5,110 | 19,040 6,040 | 22.4 26.2 | 26.2 27.6 | 29.1 21.9 | 33.3 23.5 |  |  |  |  |  |  |  |  |  |  |
|  | VB | 313.2 1095 | 0.33 | 0. 36 | 12, 280 | 13,510 | 25.3 | 26.5 | ${ }_{26.5}^{26.9}$ | 27.9 | 10-19.9 | 223.2 | 0.28 0.39 | 0. 28 | $\begin{array}{r} \text { 6. } 090 \\ 13,490 \end{array}$ | 6.650 14,370 | 27.2 24.3 | 28.3 25.9 | 22.4 | 23.5 29.4 |
|  | AM | $1,095.9$ 285.6 | 1.11 0.25 | 2.27 0.33 | $\begin{aligned} & 15,640 \\ & 10,240 \end{aligned}$ | $\begin{aligned} & 19,930 \\ & 11,360 \end{aligned}$ | 18.5 25.4 | $\begin{array}{r} 22.9 \\ 26.4 \end{array}$ | 29.6 25.6 | 38.4 26.8 | 20-29.9 | 407.0 | 0.84 | 1. 25 | 22, 130 | 23, 720 | 17.8 | 21.1 | 33. 3 | 38.2 |
| 3 -axle: | A M | 1,996. 4 | 0.83 | 1. 72 | 21,650 | 29, 480 | 18.2 | 21.4 | 32. 5 | 39.3 | (10-19.9 | 543.3 |  |  |  |  |  |  |  |  |
| Heary | All | 1,818.2 | 0.88 | 1.61 | 20,600 | 27,730 | 19.1 | 22. 5 | 31.3 |  | 20-29.9 9 | 565.7 | 1.16 | 1.14 | $\begin{aligned} & 15,320 \\ & 21,760 \end{aligned}$ | $\begin{aligned} & 17,450 \\ & 23,970 \end{aligned}$ | 21.4 17.8 | $\begin{aligned} & 25.8 \\ & 22.4 \end{aligned}$ | $\begin{array}{r} 26.3 \\ 34.0 \end{array}$ | $\begin{aligned} & 30.5 \\ & 38.4 \end{aligned}$ |
| All capacity groups.- | $\left\{\begin{array}{l} \mathrm{VBH} \\ \mathrm{AM} . \\ \mathrm{All} .- \end{array}\right.$ | $1,888.0$ $1,918.8$ $1,613.7$ | 1.18 <br> 0.84 <br> 0.80 <br> 0.8 <br>  | 1.78 1.82 1.53 | 13,690 21,870 20,370 | 19,520 29,400 26,700 | $\begin{aligned} & 19.1 \\ & 23.5 \\ & 18.1 \\ & 19.5 \end{aligned}$ | 28.1 21.3 22.7 | $\begin{array}{r} 21.0 \\ 25.5 \\ 32.9 \\ 31.3 \end{array}$ | 37.5 28.5 40.1 37.3 | $\left\{\begin{array}{l}10-19.9 \\ 20-29.9\end{array}\right.$ | $\begin{aligned} & 550.6 \\ & 517.3 \end{aligned}$ | $\begin{aligned} & 0.92 \\ & 1.09 \end{aligned}$ | $\begin{aligned} & 0.89 \\ & 1.19 \end{aligned}$ | $\begin{aligned} & 14,900 \\ & 22,060 \end{aligned}$ | $\begin{aligned} & 17,060 \\ & 24,080 \end{aligned}$ | $\begin{aligned} & 22.0 \\ & 18.6 \end{aligned}$ | $\begin{aligned} & 25.6 \\ & 22.8 \end{aligned}$ | $\begin{array}{r} 26.7 \\ 32.9 \end{array}$ | $\begin{aligned} & 30.1 \\ & 37.5 \end{aligned}$ |
| Truck-tractors with semitrailers: 2-S1: |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| edium | $\left\{\begin{array}{l} \text { VBH-VM } \\ \text { AM-AM } \\ \text { AHI } \end{array}\right.$ | $\begin{aligned} & 1,769.6 \\ & 1,377.7 \\ & 1,032.3 \end{aligned}$ | $\begin{aligned} & 1.34 \\ & 1.35 \\ & 0.88 \end{aligned}$ | 1.93 <br> 1.33 <br> 1.07 <br> 0 | $\begin{aligned} & 19,130 \\ & 20,120 \\ & 20,630 \end{aligned}$ | $\begin{aligned} & 26,070 \\ & 25,520 \\ & 24,680 \end{aligned}$ | $\begin{aligned} & 21.7 \\ & 24.2 \\ & 23.7 \end{aligned}$ | $\begin{aligned} & 26.9 \\ & 29.4 \\ & 27.1 \end{aligned}$ | $\begin{aligned} & 30.2 \\ & 28.5 \\ & 30.1 \end{aligned}$ | $\begin{aligned} & 37.8 \\ & 33.7 \\ & 34.3 \end{aligned}$ | $\left\{\begin{array}{l} 10-19.9 \\ 20-29.9 \end{array}\right.$ | $\begin{aligned} & 398.3 \\ & 908.3 \end{aligned}$ | $\begin{aligned} & 0.90 \\ & 1.36 \end{aligned}$ | $\begin{aligned} & \text { 1. } 48 \\ & 1.03 \end{aligned}$ | $\begin{aligned} & 16,440 \\ & 22,970 \end{aligned}$ | $\begin{aligned} & 18,000 \\ & 26,530 \end{aligned}$ | $27.0$ $20.2$ | $\begin{aligned} & 30.6 \\ & 25.6 \end{aligned}$ | $\begin{aligned} & 26.8 \\ & 30.6 \end{aligned}$ | $\begin{aligned} & 32.6 \\ & 34.6 \end{aligned}$ |
| Heavy | AM-AM | 1,043. 6 | 0.85 | 0.94 | 23, 700 | 27, 790 | 21.9 | 25.3 | 31.4 | 35.0 | $\left\{\begin{array}{l} 10-19.9 \\ 20-29.9 \\ 30-39.9 \end{array}\right.$ | $\begin{aligned} & 447.9 \\ & 533.8 \\ & 738.6 \end{aligned}$ | $\begin{aligned} & 1.47 \\ & 1.00 \\ & 1.23 \end{aligned}$ | $\begin{aligned} & 1.74 \\ & 1.17 \\ & 1.42 \end{aligned}$ | $\begin{array}{r} \begin{array}{r} 17,10 \\ 22,580 \\ 32,320 \end{array} \end{array}$ | $\begin{aligned} & 18,860 \\ & 24,670 \\ & 35,210 \end{aligned}$ | $\begin{aligned} & 24.1 \\ & 23.1 \\ & 16.0 \end{aligned}$ | $\begin{aligned} & 29.9 \\ & 27.1 \\ & 20.8 \end{aligned}$ | $\begin{aligned} & 26.5 \\ & 29.7 \end{aligned}$ | $\begin{aligned} & 33.3 \\ & 34.3 \\ & 40.6 \end{aligned}$ |
| All capacitygroups.... | All ${ }^{\text {VBH-VM. }}$ | 1,012.9 | 0.80 1.28 | 0.87 1.76 | 23,890 21,020 | 27,860 28,820 | 21.9 20.8 | 25. 25.8 | 31.5 31.5 | 34.9 38.3 | 10-19.9 | 300.8 |  |  |  |  |  |  |  |  |
|  | A M-AM. | 852.0 | 0.73 | 0.77 | 23, 240 | 26,580 | 23.0 | 25.8 | 31.1 | 34.1 | 20-29.9 | 467.8 | 0. 82 | 0.85 | 16,930 23,090 | 18,110 24,920 | 26.6 22.7 | 25.7 | 27.6 30.5 | 32.0 33.9 |
|  | ȦII | 744.2 | 0.60 | 0.67 | 23,070 | 25,990 | 23.1 | 25.5 | 31.5 | 34.1 | 30-39.9 |  | 0.98 | . 53 | 33,030 | 35,080 | 17.0 | 20.8 | 35.4 | 41.4 |
| 2-S2: | M-AM | 4,435. 3 |  |  |  |  |  |  |  | 38.0 |  |  |  |  |  |  |  |  |  |  |
| Heavy ------------ | A 11 | 3,805. 2 | 1.43 | 1.77 | 29,720 | 44, 630 | 18.9 | 24.5 | 31.3 | 38.3 |  |  |  |  |  |  |  |  |  |  |
|  | AM-A M | 975.1 | 0. 45 | 0.57 | 37, 560 | 41,380 | 20.5 | 22.3 | 35.0 | 37.2 | $\left\{\begin{array}{l} 20-29.9 \\ 30-39.9 \\ 40-49.9 \\ 50-59.9 \end{array}\right.$ | $\begin{aligned} & 353.0 \\ & 525.4 \\ & 43.3 \\ & 326.8 \end{aligned}$ | $\begin{aligned} & 0.72 \\ & 0.72 \\ & 0.90 \\ & 0.57 \end{aligned}$ | $\begin{aligned} & 0.86 \\ & 0.92 \\ & 0.80 \\ & 1.10 \end{aligned}$ | $\begin{aligned} & 23,510 \\ & 34,620 \\ & 43,780 \\ & 54,250 \end{aligned}$ | $\begin{aligned} & 24,89 \\ & 36,680 \\ & 45,520 \\ & 55,530 \end{aligned}$ | $\begin{aligned} & 24.5 \\ & 20.7 \\ & 19.6 \\ & 15.4 \end{aligned}$ | $\begin{aligned} & 27.3 \\ & 23.5 \\ & 23.2 \\ & 17.6 \end{aligned}$ | $\begin{aligned} & 30.2 \\ & 32.6 \\ & 33.7 \\ & 39.9 \end{aligned}$ | $\begin{aligned} & 33.6 \\ & 36.2 \\ & 36.9 \\ & 44.3 \end{aligned}$ |
|  | All | 973.1 | ${ }_{0}^{0.45}$ | 0.57 | 37,380 | 41, 190 | 20.6 | 22.4 | 34.9 | 37.1 |  |  |  |  |  |  |  |  |  |  |
| All capacity groups. | AM-AM | 956.1 | 0.44 | 0.55 | 37, 520 | 41,270 | 20.6 | 22.4 | 34.9 | 37.1 | $\left\{\begin{array}{l} 20-29.9 \\ 30-39.9 \\ 40-49.9 \\ 50-59.9 \end{array}\right.$ | 333.7 495.1 445.4 310.8 | $\begin{aligned} & 0.69 \\ & 0.69 \\ & 0.86 \\ & 0.54 \end{aligned}$ | 0.83 0.88 0.81 1.04 | $\begin{aligned} & 23,600 \\ & 34,600 \\ & 43,930 \\ & 54,330 \end{aligned}$ | $\begin{aligned} & 24,910 \\ & 36,620 \\ & 45,680 \\ & 55,550 \end{aligned}$ | $\begin{aligned} & 24.6 \\ & 20.7 \\ & 19.4 \\ & 15.3 \end{aligned}$ | $\begin{aligned} & 27.3 \\ & 23.4 \\ & 22.8 \\ & 17.5 \end{aligned}$ | 30.3 32.8 34.0 40.1 | 33.5 36.2 37.2 44.1 |
| 3-52: | All | 947.7 | 0.43 | 0.55 | 37, 230 | 40,950 | 20.7 | 22.3 | 34.8 | 37.0 |  |  |  |  |  |  |  |  |  |  |
|  | (AM-AM | 1,895.9 | 0.70 | 0.94 | 46,630 | 54, 060 | 20.3 | 23.1 | 36.1 | 39.7 | 20-29.9 | 496. 9 | 1. 36 | 1. 25 | 25,830 | 27,780 | 24.9 | 30.3 | 32.0 |  |
| ILeavy -..---..- |  |  |  |  |  |  |  |  |  |  | 50-59.9 | 738.3 | 1.18 |  | 32,180 54,590 | 34,970 57,490 | 25.6 18.6 | 30.1 23.2 | 29.5 33.9 | 33.9 41.5 |
|  |  |  |  |  |  |  |  |  |  |  | $\begin{aligned} & 60-69.9 \\ & 70-79.9 \end{aligned}$ | 675.9 778.3 | 0.85 1.00 | 1. ${ }_{\text {1. }} 1.06$ | 63,380 71,580 | 66,030 74,630 | 16.1 13.5 | 19.5 | 36.6 39.2 | 40.8 48.6 |
|  | A | 1,895. 3 | 0. 71 | 0.93 | 46,360 | 53,790 | 20.4 | 23.2 | 36.1 | 39.7 |  |  |  |  |  |  |  |  |  |  |
| All capacity groups.- | A M-A | 1.889.9 |  | 0.97 |  | 54,270 |  |  |  |  |  | 496.9 712.3 738.3 675.9 732.5 | $\begin{aligned} & 1.36 \\ & 1.15 \\ & 1.18 \\ & 0.85 \\ & 1.02 \end{aligned}$ | 1.25 1.13 1.95 1.06 2.65 | $\begin{aligned} & \begin{array}{l} 5,830 \\ 32,180 \\ 54,590 \\ 63,380 \\ -1,160 \end{array} \end{aligned}$ | $\begin{aligned} & 27,780 \\ & 34,970 \\ & 57,490 \\ & 66,300 \\ & 74,510 \end{aligned}$ | $\begin{aligned} & 24.9 \\ & 25.6 \\ & 18.6 \\ & 16.1 \\ & 13 . \end{aligned}$ | $\begin{aligned} & 30.3 \\ & 30.1 \\ & 23.2 \\ & 19.5 \\ & 17 \end{aligned}$ | 32.0 29.5 3.9 36.9 36.6 40.2 | 36.9 33.9 41.5 40.8 50.6 |
|  | All | 1,589.6 | 0.71 | 0.97 | 46, 600 | 54,010 | 20.3 | 23.1 | 36.3 | 40.1 |  |  |  |  |  |  |  |  |  |  |
| Trucks with full trailers: 3-2: | A-- | 1, 38.6 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | AM-AM | $4,66^{\circ} .3$ | 1. 75 | 1.86 | 39,820 | 58,110 | 19.7 | 26.5 | 37.7 | 44.9 | $\left\{\begin{array}{l} 20-29.9 \\ 70-79.9 \end{array}\right.$ | $\begin{aligned} & 767.5 \\ & 337.3 \end{aligned}$ | $\begin{aligned} & 0.84 \\ & 1.74 \end{aligned}$ | $\begin{aligned} & 1.33 \\ & 1.99 \end{aligned}$ | $\begin{aligned} & 24,080 \\ & 75,430 \end{aligned}$ | $\begin{aligned} & \frac{27,090}{76,750} \end{aligned}$ | $\begin{array}{r} 29.6 \\ 12.2 \end{array}$ | $\begin{aligned} & 32.9 \\ & 19.0 \end{aligned}$ | $\begin{aligned} & 31.3 \\ & 45.3 \end{aligned}$ | $\begin{aligned} & 36.5 \\ & 53.1 \end{aligned}$ |
| Truck-tractors with semitrailers and full trailers: 2-S1-2: Heavy | AM-AM- | 3,156.0 | 0.98 | 1. 69 | 54,360 | 66,740 | 17.2 | 21.0 | 43.2 | 49.8 | 70-79.9 | 379.0 | 0.56 | 2.08 | 75,540 | 77,030 | 13.8 | 16.0 | 48.6 | 56.8 |
| All capacity groups. All other than 2-S1-2: Heavy. | All.-.....- | $3,173.0$ $10,236.0$ | 0.96 1.81 | 1.66 3.40 | 53,620 60,380 | 66,060 100,500 | 17.2 16.8 | 21.0 23.8 | 43.2 38.1 | 49.8 51.5 |  |  |  |  |  |  |  |  |  |  |
| All capacity groups. | $\begin{aligned} & \text { AM- } \\ & \text { AM- } \end{aligned}$ A M. | 9, 494.9 | 1.76 | 3.21 | 61,620 | 98, 840 | 16.4 | 23.2 | 39.1 | 51.7 |  |  |  |  |  |  |  |  |  |  |
| Trucks with full trailers and truck-tractors with semitrailers and full trailers: |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Heavy |  |  |  |  |  |  |  |  |  |  | $\left\{\begin{array}{l} 20-29.9 \\ 30-39.9 \\ 70-99.9 \end{array}\right.$ | $\begin{array}{r} 471.1 \\ 7 \times 9.8 \\ 288.0 \end{array}$ | $\begin{aligned} & 0.83 \\ & 1.04 \\ & 0.58 \end{aligned}$ | $\begin{aligned} & 0.96 \\ & 1.23 \\ & 1.57 \end{aligned}$ | $\begin{aligned} & 24,860 \\ & 32,680 \\ & 75,610 \end{aligned}$ | $\begin{aligned} & 26,710 \\ & 35,7019 \\ & 36,740 \end{aligned}$ | $\begin{aligned} & 28.6 \\ & 25.3 \\ & 14.1 \end{aligned}$ | $\begin{aligned} & 31.8 \\ & 29.3 \\ & 16.3 \end{aligned}$ | $\begin{aligned} & 32.7 \\ & 32.2 \\ & 48.6 \end{aligned}$ | $\begin{aligned} & 36.5 \\ & 37.0 \\ & 54.8 \end{aligned}$ |

[^3]
# Relations of Gross Weights and Horsepowers of Commercial Vehicle 

BY THE OFFICE OF<br>RESEARCH AND DEVELOPMENT<br>BUREAU OF PUBLIC ROADS

Reported by ${ }^{1}$ JOHN M. WRIGHT and SAMUEL C. TIGNO,<br>Highway Research Enginee Traffic Systems Divisi

Results of a study on the relation between gross weight and net engine horsepower of commercial vehicles are presented in this article. Data from the braking performance study were used to update current information on weightpower ratios of trucks and to investigate the trend in these ratios since 1919. A total of 1,026 commercial vehicles, in a large variety of types, weights, and horsepowers were sampled in three States from routes having a heavy concentration of commercial vehicles.
Data from the study were used to determine the effect of weight-power ratio requirements on the trucking industry and to determine the percentage of whicles affected by a minimum performance requirement. The data collected in the study indicate that the dissimilarity in performance of passenger cars and commercial vehicles is lessening. There is a trend toward decreasing weight-power ratios and a performance requirement of 400 pounds per horsepower would affect only a small percentage of the commercial vehicles. However, a substantial reduction in the weight-pouer ratio is still necessary to put passenger and commercial vehicles on similar performance levels.

## Introduction

TIIE BUREAU of Public Roads periodic braking performance study made in 1963 also provided information for determining the ratios of commereial vehicle gross weight to net engine horsepower. An engine net horsepower rating for each truck or trailer combination trested wats also recorded. Field observations were made in Maryland, Michigan, and California on routes having a heary concentration of commercial vehicles. A total sample of 1,026 commercial vehicles in a large variety of types, weights, and horsepowers was investigated.

A study of weight-power ratios published in $1957(1)^{2}$ included data collected in 194!), 1950, and 1955. The 1950 data, collected in conjunction with the amual truck weight survey, contained information on 10,726 trucks in 39 States. The 1949 and 1955 data, were obtained from brake tests on 782 and 862 commereial vehieles, respectively, in the same States as the 1963 brake study. The 196:3 brake test data have beell used to update the weight-power ratio information published in 19.57 and to indicate the trend in the ratios.

It is believed that a performanee requirement of 400 pounds per horsepower for

Presented at the Octoler 1964 meeting of National Transportat ion, Powerplant, and Fuels and Lals ricants Meeting, of the societ y of Automot ive Engineers, Inc., Balt imore. 11 d . ${ }^{2}$ Relation Belureen (iross Weights of Hotor Trucks and Their Highway Research, Vol, 29. No, 10, Oetober 195\%, pp, 233 -238.
commercial vehicle operation would improve the weight-power ratios, but a substantial reduction in this ratio will be required before the two types of vehicles attain similar performance levels. For example, large horsepowers are required for trucks to maintain a high speed on grades. A trailer combination having a gross weight of 100,000 pounds and powered by a 250 -net-horsepower engine can maintain a speed of $50 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. on the level, but up a 3 -percent grade only $20 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. To maintain the $50 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. speed up the 3percent grade, this vehicle would require an engine capable of producing a net horsepower of 700 .

Although production of highway commercial vehicles equipped with 700 -horsepower engines may be remote, the trend is toward larger engines and smaller weight-horsepower ratios. Furthermore, the authors beliewe industry is capable of producing engines larger than those now in use. In addition, information has been developed to show that an increase in the average road speeds is economically justifiable for owners who caln use their equipment advantageously during the time saved (HRB Bulletin 301, Line-Haul Trucking Costs in Relation 10 I'ehicle (rioss Weights)

## Conclusions

()n the basis of information gathered in the study reported here, the authors conclude that commercial vehicles having larger horsepower engines soon may be operating on the high-
ways. Use of these larger engines would $n$. row the gap between the performance of $p$ : senger cars and commercial vehicles. Crite developed during earlier studies on whi performance and still accepted in designi highways are: (1) operating characteristics commercial vehicles and passenger cars are 1 similar; (2) these two types of vehicles canr. be designed any time soon to similar perfor ance standards without an injustice being do to one or both; (3) public interest requires th: highways be adequately designed and oc structed to serve both passenger wehicles al commercial vehicles; (4) by appropriate hig way design, the highways required for opel tion of both types of vehicles can be design so that these vehicles can operate without u due movement restrictions.

Analysis of the data collected during $t$ study on the weight-horsepower ratios has plvided information from which the authe concluded that the performance gap is bei narrowed. The weight-power ratios of cols mercial vehicles decreased 12 percent fri 1949 to 1955 and 28 percent from 1955 to $19 t$.

## Purpose of Study

The primary purpose of the study was update information on weight-power rati of commereial vehicles in order to analy traveltime, grade-climbing ability, and : celerating ability of trucks. Another purpe was to investigate the trend in weight-pow. ratios, based on 1949 and 1955 brake tes, and 1950 truck weight survey informatic Data from the 1963 study may also be us! to determine the effect of minimum weigh power ratio requirements on the trucki industry. It can provide information the percentage of vehicles affeeted by minimum performance requirement. For $\epsilon$ ample, a performance requirement of $4^{\prime}$ pounds gross weight per net horsepower e: be translated into grade-climbing ability 1 . cause it is inversely proportional to the rat: A weight-power ratio of 400 is approximate equal to 20 m.p.h. on a 3 -percent grade.

Nany believe that the result of a minimul performance requirement would be bett balance between the vehicle weight the load for which its tires, brakes, it other components were designed. It doubtful that commercial vehicles cout
ver be required to maintain the same speed h grades as passenger cars. Nevertheless minimum performance requirement may rovide the highway engineer with a level vehicle performance on which to base ighw:y design standards conducive to lifer and more efficient movement of traffic.

## Analysis Procedure

The first step in the analysis of the data Hected was to determine the net horseJwer of each truck in the sample. When:er possible, this was obtained in the field om the vehicle manufacturers rating plate. he net horsepower for unrated vehicles as determined from the vehicle specificaons of individual manufacturers and the utomobile Manufacturers Association. hen only gross horsepower could be deterinerd, the net horsepower was assumed i) be 90 percent of that value. When two more horsepower options were available 4 ar aiven model and it was not possible determine which was installed in the frticular vehicle, the net horsepower of te smaller engine was used for computing ie ratio.
After computation of weight-power ratios, le ratios were grouped according to vehicle pe and gross weight. The average net orsepower, the average gross weight, and te average weight-power ratio for each vehicle "pe were computed. The gross weights, 't horsepowers, and weight-power ratios "r each vehicle type were tabulated also. 'umulative frequency distributions of weightWwer ratios were made for each vehicle pe by grouping the weight-power ratios class intervals of 50 pounds gross weight ir net horsepower. The 15 th, 50 th, and iith percentiles of the frequency distributions imin 1955 and 1963 were tabulated and in mpared.
An analysis was made to determine the lation between the weight-power ratio ad the gross weight of the vehicles regardyiss of rehicle type. The vehicles were mouped in intervals of 10,000 pounds gross ight and the average ratio was calculated ir each interval group. These weight1) wer ratios were plotted in relation to the boss weight and compared with similar firves derived from 1949 and 1955 data. A parate analysis was made for only loaded thicles in the 1963 braking study. Loaded Whicles were those that carried any cargo
payload. Of the 1,026 vehicles, 634 "re loaded. The same procedure for analis of loaded vehicles was used as for the ital sample of empty and loaded vehicles.

## Survey Results

A summary of the horsepowers, weights, ad weight-power ratios for each vehicle 'pe is shown in figure 1 and table 1 . Two 1 lethods of listing the data were used in Hure 1: average for all vehicles and average oulr loaded vehicles only. Gross weights, If it horsepowers, and weight-power ratios wicreased as the number of axles increased



Figure 1.-Average weight-power ratios and gross weights for commercial vehicles, 1963 brake test.


Figure 2.-Cumulative frequency distributions of weight-power ratios for all commercial vehicles, 1955 brake test.
up to is axles, as shown in table 1. For vehicles having 5 or more axles, the measures remained fairly constant. Thus, a large variation in hill climbing and ascelerating ability wats indicated for the different wehicle types. The smaller weight-power ratios were generally computed for empty vehicles having large engines. For example, an empty $3-\mathrm{S} 2$ trailer combination having a 310 net horsepower engine weighed 29,100 pounds and had the smallest weight-power ratio, 94, for any of the $3-52$ trailer combinations tested. The 310 net horsepower also was the largest horsepower for any vehicles tested in the 1963 braking performance study.

Data for the loaded vehicles only are shown in table 1. Although the average weight and the lowest limits of the weight range were larger for the loaded vehicles than for the total of all vehicles, net horsepower remained nearly constant for both loaded only and the total of all vehicles tested. Therefore, the average weight-power ratio and the lowest weight-power ratios were also larger for the loaded vehicle sample than for the total vehicle sample.

Larger weight-power ratios occurred when vehicles having small engines were heavily loaded. A 3-52 trailer combination having a gross weight of 94,650 pounds and a net engine horsepower of 135 had a weightpower ratio of 701 , the largest ratio for any vehicle in the 1963 brake study. This particular vehicle was operating under a special permit because it had tandem axle weights in excess of the legal limit for the State in which it was operating. However, it is possible to transport extremely heavy loads and remain within the legal weight limits of the State, as illustrated by a $3-$ S3- 5 trailer combination having a gross weight of 132,570 pounds and a weight-power ratio of 567 .

Cumulative frequency distributions for all vehicle types for 1955 and 1963 are shown in figures 2 and 3 , respectively. The summary in table 2 of the cumulative frequency distributions at the 15 th, 50 th, and 85 th percentiles shows a reduction in the ratios from the 1955 to the 1963 study for all vehicle types. The percentage change at the 50 th percentile was 28 percent for 2-axle, singletired trucks; 36 percent for 2-axle, dual-tired trucks; 45 percent for 3 -axle trucks; 48 percent for 2-S1 trailer combinations; 27 percent for 2-52 trailer combinations; and 31 percent for all other trailer combinations. The average reduction in ratios for all vehicle types was approximately 30 percent at the 15 th and 50 th pereentiles and 25 percent at the S5th percentile.

Cumulative frequency distributions of weight-power ratios for trailer combinations 3-S2 and 2-S1-2 from the 1963 study are shown in figure 4. These curves show data separated from that shown by the curve labeled other in figure 2 . The sample size for the 1955 study was not large enough for such a breakdown. The irregularity in the curve for the 2-S1-2 trailer combinations (fig. 4) occurred because nearly all of these trailer


Figure 3.-Cumulative frequency distributions of weight-power ratios for all commercial vehicles, 1963 brake test.


Figure 4.-Cumulative frequency distributions of weight-power ratios for ai 3-S2 and 2-S1-2 trailer combinations, 1963 brake test.
combinations either were traveling empty or heavily loaded. The sample vehicles in the middle-weight range was small; only 5 of 51 had gross weights within the range of 35,000 to 70,000 pounds.

Cumulative frequency distributions weight-power ratios for only loaded vehicl the 1963 study are shown in figure 5 by ve type. The curve designated as other incl $3-\mathrm{S} 1,3-\mathrm{S} 2,2-2,2-\mathrm{S} 1-2$, and all other $\operatorname{tr}$
ble 1.-Range and average of gross weights, net horsepowers, and weight-power ratios for commercial vehicles weighed in 1963 brake performance study

| Jommercial vehicles | All commercial vehicles tested in 1963 brake study |  |  |  |  |  | Loaded commercial vehicles tested in 1963 brake study |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Gross weight |  | Net horsepower |  | Weightpower ratio |  | Gross weight |  | Net <br> horsepower |  | Weightpower ratio |  |
|  | Range | $\begin{aligned} & \text { Aver- } \\ & \text { age } \end{aligned}$ | Range | $\begin{aligned} & \text { Aver- } \\ & \text { age } \end{aligned}$ | Range | $\begin{aligned} & \text { Aver- } \\ & \text { age } \end{aligned}$ | Range | $\begin{aligned} & \text { Aver- } \\ & \text { age } \end{aligned}$ | Range | Average | Range | $\begin{gathered} \text { Aver- } \\ \text { age } \end{gathered}$ |
|  | Pounds | Pounds | IIorsepower | Horsepower | Ratio | Ratio | Pounds | Pounds | Horsepower | Horsepower | Ratio | Ratio |
| - tired) | 2, 545-11, 120 | 4,795 | 50-165 | 109 | 24-128 | 44 | 3, 270-11, 120 | 5, 275 | 63-165 | 108 | 29-128 | 49 |
| tired) | 5, 700-31, 410 | 13. 230 | 80-198 | 136 | 42-267 | 97 | 6. 0:20-31,410 | 15, 425 | 80-198 | 136 | 45-267 | 113 |
|  | $11,000-47,410$ $13,000-45,400$ | 22, 78.63 | $\xrightarrow{95-222}$ |  |  |  | 11, 000-47, 410 | 27,460 28,700 | $95-222$ $118-230$ | $\begin{aligned} & 157 \\ & 167 \end{aligned}$ | $\begin{aligned} & 82-282 \\ & 99-304 \end{aligned}$ | 175 172 |
| 2-82 | 15, 900-64, 805 | 39, 030 | 110-238 | 172 | 89-427 | 227 | 19, $270-64,805$ | 44, 625 | 110-235 | 172 | 120-427 | $\stackrel{1}{259}$ |
| 3-52 | 22, 010-94, 650 | 50, 625 | 128-310 | 184 | 94-701 | 275 | 27, 240-94, 650 | 60,775 | 134-255 | 185 | 151-701 | 329 |
|  | 22, 400-78, 200 | 48, 070 | 128-250 | 184 | 93-511 | 261 | 49, 600-78, 200 | 73, 150 | 150-209 | 182 | 329-511 | 403 |
| 2-81-2 | 24, 500-82, 770 | 59, 595 | 130-235 | 186 | 111-590 | 321 | 36, 600-82, 770 | 73, 685 | 134-235 | 185 | 203-590 | 398 |
| combina- tions ${ }^{1}$. | 16, 000-132, 570 | 54, 995 | 153-288 | 188 | 88-625 | 292 | 16, 000-132, 570 | 67, 285 | 133-234 | 187 | 88-625 | 359 |

: Includes 3-S2 and 2-S1-2 and other trailer combinations not listed specifically.
nbinations having 5 or more axles. The 132 and $2-$ S1-2 types are shown separately pause they are the largest groups for which I: a is contained in the curve labeled other. Le 15 th, 50 th, and 85 th percentiles of the nulative frequency distributions for the $\rightarrow$ ded vehicles tested in 1963 are summarized atable 3. These ratios follow a pattern simIr to that for the total of vehicles tested in Ti33, except that the ratios are larger when oly loaded vehicles are considered.

- In figure 6 the trend in weight-power ratios H.m 1949 to 1963 is illustrated. The curves a: based on average data for all commercial vicles weighed in the brake studies of 1949 , 155 , and 1963. The average ratios for all -hicles sampled in the 1950 truck weight sur$v y$ are indicated by the triangular symbols in fiure 6. Average ratios for the 1950 truck ight survey closely follow the curve for the 149 brake test data; this indicates the validity - the smaller sample of vehicles. The aver* ratios for all vehicles sampled in a differ--3t, but related, study conducted in 1964 near loodbridge, Va., also are shown in figure 6. Jiese data on 408 trucks are indicated by the acular symbols. Data collected at Woodridge closely approximate the 1963 brake test -dta and, therefore, substantiate the results c the 1963 brake test.
The reduction in the weight-horsepower rtios from 1949 to 1955 amounted to about 15 ircent for vehicles having gross weights less tan 40,000 pounds. Above that weight, the 'range decreased to about 8 percent at 80,000 runds. From 1955 to 1963 , the reduction iounted to about 25 percent for gross rights up to 40,000 pounds. The change §adually decreased to about 16 percent at ins,000 pounds gross weight.

The 1963 test data on loaded trucks also tre analyzed. The curve obtained closely A proximated the curve for all trucks in the risimple. At weights of less than 40,000
pounds, the difference in the two curves was 2 percent or less. For weights of more than 40,000 pounds, the two curves are identical. Therefore, only one curve is shown.

The trend in average weight-power ratios by vehicle type from 1949 to 1963 is shown in table 4. The variation in percentage change from 1949 to 1955 and from 1950 to 1955 was small, except when the sample size was small. The comparison of 1949 and 1955 data showed that the largest reductions in ratio occurred for 2-axle, single-tired trucks and 2-S2 and

Table 2.-Comparison of weight-power ratios ly percentiles from cumulative frequency distributions for $\mathbf{1 9 5 5}$ and 1963

| Commercial vehicles | Weight-power ratio, pounds per horsepower |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 15th percentile |  | 50th percentile |  | 85th percentile |  |
|  | 1955 | 1963 | 1955 | 1963 | 1955 | 1983 |
| 2 (single-tired) | 41 | 32 | 58 | 42 | 85 | 56 |
| 2 (dual-tired). | 73 | 64 | 135 | 87 | 208 | 14.2 |
| 3. | $13 \%$ | 88 | $\because 45$ | 135 | 306 | 208 |
| $2-51$ | 161 | 108 | 256 | 133 | 376 | 204 |
| 2-S2 | 186 | 126 | 300 | 218 | 406 | 327 |
| 3-S2 | --. | 157 | --. | 272 | -.- | 377 |
| $2-\mathrm{S} 1-2$ <br> Other trailer |  | 141 |  | 360 | --. | 431 |
| combinations ${ }^{1}$-... | 232 | 138 | 400 | 278 | 531 | 428 |

${ }^{1}$ Includes 3-52 and 2-S1-2 and other trailer combinations not listed specifically.

Table 3.-Weight-power ratios for loaded vehicles from cumulative frequency distributions, by percentiles, 1963

| Commercial vehicles | Weight-power ratio, pounds per horsepower |  |  |
| :---: | :---: | :---: | :---: |
|  | 15 percentile | 50 percentile | 85 percentile |
| 2 (single-tired) | 37 | 45 | 60 |
| 2 (dual-tired) ---- | 75 | 106 | 157 |
|  | 110 | 125 | 243 |
| 2-S1 | 117 | 116 | 223 |
| 2-S2 | 180 | 25. | 346 |
| 3-S2 | 247 | 315 | 408 |
| ${ }^{2-S 1-2}$ | 338 | 388 | 454 |
| Other trailer combinations ${ }^{1}$ | 251 | 354 | 452 |

${ }^{1}$ Includes $3-52$ and $2-S 1-2$ and other trailer combina. tions not listed specifically.

3- 82 trailer combinations. The ratio increased from 1949 to 1955 for 3 -anle trucks and 2-3, 3-2, and 2-s1-2 trater combinations. The ratio for 2 -asle, dual-tired trucks, did not change. A reduction in the ratio occurred for all vehicle types from 1955 to 1963, the largest pereentage reductions were for the 2-axle, clual-tired, and 3-axle trucks, and 2-S1 trailer combinations. The overall reduction in the ratio from 1949 to 1955 was about 12 percent. The corresponding reduction from 1955 to 1963 wats approximately 28 percent.

The percentages of vehicles sampled in 1955 and $1!963$ that could not meet performance requirements are listed in table 5. Comparison of these pereentages shows considerable change. Percentages for $3-52$ and $2-\$ 1-2$ trailer combinations are not shown for 1955 becanse of inadequate samples. In 1955, 50 pereent of the vehicles having 5 or more axles -14 pereent of the total sample-had weight-power ratios of more than 400 pounds per horsepower. In 1963 , only 20 percent of vehicles with 5 or more axles, and 5 percent of the total sample, had weight-power ratios of more than 400 . The percentage of the loaded rehicles sampled in 1963 that could not meet the different performance requirements are shown in table 6 . These percentages were taken from figure 5. In 1963, 30 pereent of the loaded vehicles with 5 or more axles and 8 percent of the total sample of loaded vehicles had weight-power ratios of more than 400 .


Figure 6.-Trend in weight-power ratios from 19.19 to 1963 based on average dat for all types of commercial vehicles.

Table 4.-Average weight-power ratios for all vehicles by types for $1949,1950,1955$, and 1963

| Commercial vehicles | Number of vehicles |  |  |  | A verage weight-power ratios |  |  |  | Percentage reduction of weight-power ratios |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1949 | 1950 | 1955 | 1963 | 1949 | 1950 | 1955 | 1963 | 1949-55 | 1950-55 | 1955-63 |
| 2 (single-tired) | 19 | 239 | 99 | 130 | 81 | 75 | 57 | 44 | 30 | 24 | 23 |
| $\frac{2}{3}$ (clual-tires) | 275 38 | ${ }_{263}{ }^{3.4}$ | 278 | 312 | 142 | 135 244 | 142 | 145 | 0 -2 | -5 5 | 32 37 |
| 2-81 | 228 | 3. 900 | 117 | 108 | 291 | 294 | 2614 | 149 | 9 | 10 | 44 |
| 2-82 | 87 | 1. 991 | 145 | 217 | 369 | $35 \%$ | 301 | 227 | 18 | 16 | 25 |
| 3-82 | 46 | 483 | 57 | 112 | 422 | 411 | 348 | 275 | 18 | 15 | 21 |
| 2-3, 3-2, and 2-81-2 | 51 | 136 | 71 | 78 | 394 | 384 | 418 | 300 | -6 | -9 | 28 |
| Other trailer combinations ${ }^{1}$ | 38 | 72 | 34 | 27 | 428 | 421 | 3.4 | 292 | 13 | 11 | 22 |
| total. | 782 | 10.726 | 862 | 1.026 |  |  |  |  |  |  |  |
| weighten ayerages. |  |  |  |  | 260 | 253 | 228 | 165 | 12 | 10 | 28 |

${ }^{1}$ Includes trailer combinations not listed specifically.

Table 5 .-Percentage of all vehicles of given types weighed in the 1955 and 1963 brake tests that could not meet indicated performance levels

| Commercial vehicles | Vehicles with weight-power ratios larger than- |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 250:1 |  | 300:1 |  | 350:1 |  | 400:1 |  | 450:1 |  | 500:1 |  |
|  | 1955 | 1963 | 1955 | 1963 | 1955 | 1963 | 1955 | 1963 | 1955 | 1963 | 1955 | 1963 |
| 2 (single-tired) |  |  |  |  | ---- | --- |  |  |  | - .-- | --... | -- |
| $\frac{2}{3}$ (dual-tired) .- |  |  | 1 | --- |  | - |  |  | - | -...- |  | -... |
| 2-31 | 53 | 1 | 34 | 1 | 20 | - | 10 |  | 2 |  | - | --- |
| 2-82 | 16 |  | 50 |  | 34 |  | 17 |  | 5 |  | 1 |  |
| 3-82 |  | 57 |  | $3 \times$ |  | 23 |  | 12 |  | 5 |  | 6 |
| 2-81--2 - - .ander- |  | 67 |  | ti5 |  | 55 |  | 18 |  | 12 |  |  |
| Other trailer combination ${ }^{1}$ | $\times 2$ | 55 | 73 | $4{ }^{\text {i }}$ | $6: 2$ | 34 | 50 | 20 | 35 | 10 | 22 | 7 |
| total. | 38 | 20 | 29 | 14 | 20 | 9 | 14 | 5 | 8 | 2 | 4 | 1 |

Table 6.-Percentage of loaded vehi weighed in the 1963 brake tests that col not meet indicated performance levels

${ }^{1}$ Includes 3-S2 and 2-S1-2 and other trailer com tions not listed specifically.

[^4]
# 0ifitracking Calculations For Trailer Combinations 

iY THE OFFICE OF<br>ESEARCH AND DEVELOPMENT IUREAU OF PUBLIC ROADS

Reported by ${ }^{1}$ HOY STEVENS,
Highway Transport Research Engineer;
SAMUEL C. TIGNOR,
Highway Research Engineer;
and JAMES F. LOJACONO,
Engineering Technician;
Traffic Systems Division

In this article the offtracking characteristics of single-unit trucks and trailer combinations are described. Offtracking results were obtained by use of scale models of vehicles making turns on radii ranging from 25 to 255 feet. Individual vehicle off trackings are influenced by three variables: the degree of turn, the length of vehicle wheelbase, and the turning radius. It was determined that the offtracking measurements of a trailer combination may be calculated by adding the offtracking measurements of the individual vehicles in the combination. Also, the offtracking is greatest when the projection of the rear axle axis passes through the turning radius center, even though the projections of the other axles on the vehicle or trailer combination do not pass through the turning radius center at the same time.

The research reported here was planned to develop a more simple, quick, and comprehensive method for calculating offtracking. This method uses a series of figures constructed to allow for direct reading and calculation of offtracking for almost all practical highway vehicles and trailer combinations. The information is given for turns of 90 degrees and 270 degrees and for outer front-wheel turning radii from 25 to 225 feet. The range of turns and turning radii covers most of the vehicle turns made on city streets and turns made at rural intersections, including at-grade intersections, diamond interchanges, and separated cloverleaf interchange ramps.

## Conclusions

On the basis of findings from the research reported here, the authors have concluded that additional research may be required. Information on offtracking for turns of different de-grees-only 90- and 270 -degrees turns were studied-can be obtained by using similar models and procedures. They suggest that perhaps studies should be made of the mane thverings required for long trailer combinations on different types and sizes of cloverleaf intersections.

Although the research results reported here indicate that width over the tires has almosit no effect on the offtracking characteristics of the outside of the outer tires of a trailer combination, additional studies may be required becaluse of offtracking of certain units. It is believed that the width over the front tires of a power vehicle having Ackermansteering may have some limiting effect on the offtracking of the vehicle.

The aththors also believe that additional irosearch is needed to define more precisely the pereentage relation between the turning radii :und the wheelbase of different trailers. Knowledge gitined from such a study would be useful to highway designers so that trailer backup) and pivot motion on $18(0$ - and $27(0$-degree turns could be prevented.

## Basis of the Study

The fundamental premise madu for the study was that: The simm of the offtracking of

[^5]degrees of turn made by the vehicle before it exited onto a tangent.

Sketches, drawings, and detailed descriptions of the minimum turning paths of specific vehicles have also been provided. Although of value this information is inadequate because easy interpolation camot be made of offtracking measurements between different types of vehicles and neither can comparisons be made of performance of vehicles of different wheelbases operated on turns of different radii. Even the sAE offtracking formulats (1) ${ }^{2}$ require the use of specific vehicle dimensions, and then only maximum offtracking measurements are obtained for a particular combination. Thus, to make a comparison of the offtracking characteristics of different vehicles or to determine the offtracking limits for some particular turning radius, a long and tedious process of individually calculating the offtracking for cach variation in vehiche dimensions is required.

Previonsly reported offtracking data have been based on measurements taken from the center of the axles of the wehicle. Although such datal may be satisfactory for automotive engineering uses, the highway engineer must add or subtract other factors. In the study reported in this article all offtracking and turning radius measurements were made to the outside of the outer tire of an axle.

[^6]the individual vehicles of a highway trailer combination closely approximates the total offtracking of the combination. The research plan included experiments with vehicle models that led to the establishment of patterns of vehicle offtracking behavior that are related to differences in wheelbase length, turning radius, and degree of turn. The final step in the research was the development of methods of plotting these data for rapid use and comparison.

Because sometimes two or more engineering organizations have defined the same terms differently and a few terms are used that have not been previously defined, the definitions in the following list and those at the front of this magazine should be considered carefully.
Angle of turn.- The angle of turn is the angle through which a vehicle travels in making a turn (2).
Axle.-For simplification, only the single term axle is used: it designates either a single axle or the centerline between fandem axles; this application depends on the vehicles being considered. The term axle can be used because the theoretical turning center of a tandem-axle assembly lies on the centerline between tandem axles.

Cramp angle.-The cramp angle is the limit of the turning ability of the front wheels of an Ackerman-type front axle and is limited by the construction of mechanical parts around the the front-axle, kingpin-pivot mechanisms. These constructions limit the degree to which the inner front wheel may be turned and also the turning of the outer front wheel.
Fifth wheel.-The fifth wheel is a lubricated bearing plate, mounted on a tractor chassis or on a trailer converter dolly chassis, arranged with an internal clutch device to engage and hold the kingpin of a trailer. The fifth wheel cluteh engages and locks upon contact with the trailer kingpin; a manual release by the driver is required to separate the trailer kingpin and the fifth wheel. Primarily, the manual fifth wheel is being used. Previously an automatic fifth wheel was attached to the trailer and connected to this landing gear, and the kingpin was mounted on the towing vehicle. Few of these automatic fifth wheels are in use now, and these few are used only in local cartage service where the semitrailers are a captive fleet. In the article on braking performance the term fifth wheel refers to a trailing, fifthwheel, distance-measuring device.
Kingpin.--The term kingpin has two different meanings in automotive design, and the precise meaning is determined by the context in which the term is used. A kinpgin of a front axle of a power vehicle is a vertical or near vertical shaft. The shaft is the pivot connecting each stub axle that carries a front wheel of a power vehicle to the rigid center of an Ackerman-type front axle. All Ackerman-type front axles have two kingpins, one at each end of the rigid center of the front axle.

A kingpin of a trailer is a vertical pivot shaft attached near the front of and on the centerline of the underside of a trailer chassis. This kingpin is surrounded by a lubricated bearing pate. It engages a fifth wheel on a towing tractor, a trailer converter dolly, or it is permanently connected to the center of an undetachable front axie of a full trailer. A trailer is pulled by and pivots around its kingpin.
Radius of inside curb.-The radius of the inside curb is the radial difference between the furning radius and the turning track width when the offtracking of the vehicle is at the maximum amount for a given turn. This shortest inside eurb radius will occur at only one point (instantaneously) on a 90 -degree turn. On a 270 -degree turn, the shortest curb radius may remain constant for some distance before the exit tangent.

Ninimum turning radius.-The minimum turning radius is the radius of the minimum turning path of the outside of the outer front tire. Vehicle manufacturers data books usually give minimum turning radius to the centerline of the outer front tire (2).

Negative offtracking.-Negative offtracking occurs during a turn in which the radius of the path of the outer rear corner of a vehicle becomes longer than the radius of the turning path of the outside of the vehicle's outer rear tire. For example, for a tractive truek or a trailer that has a cargo body extending back of the rear axle, negative offtracking occurs as the outer rear corner of the cargo body swings outside the path of the outside of the outer rear tire.

Offtracking.-Oftitracking is the path of the outside of the outer tire on a rear or trailing axle that deviates inward
toward the center of a turn from the circular path of the outside of the outer front tire, while the vehicle or trailer combination is making a turn.
Outside of tire.-The outside of a tire is the external side of a tire farthest away from the vehicle chassis.
Outside of outer tire.-The outside of the outer tire of a vehicle is the outside of the outermost tire on an axle on the outer side of a turn.

Outside of innermost rear tire.-The outside of the innermost rear tire of a vehicle is the outside of the rear tire uearest the turning radius center.

Overall length.-The overall length of a vehicle or trailer combination is the distance between the front bumper of the power vehicle and the rear bumper or guard on the rear vehicle.

Pintle hook.-A pintle hook is a vertical hook device attached to the rear of a tractive truck or to the rear of a leading (towing) semitrailer in a double trailer combination. The pintle hook engages the towing eye (ring eyelet) at the front end of the towbar of a trailer converter dolly or the towbar of a full trailer undetachable front-axle assembly.
Power vehicles.-Three general types of power vehicles are used:

- Single-unit trucks are power vehicles having Ackerman front-axle steering equipped with a cargo body but not equipped to pull a trailer.
- Tractive trucks are power vehicles with Ackerman front-axle steering equipped with a cargo body and a pintle hook that is attached to and recessed into the rear frame members so that a full trailer may be pulled.
- Tractors for commercial freight use are legally defined as truck-tractors to differentiate them from farm or industrial tractors. The single term tractor, however, is used in this article for a power vehicle of short wheelbase that is equipped with Ackerman front-wheel steering and a fifth wheel to engage and pull a semitrailer.
Rear axles of trailers.-Rear axles of trailers are attached primarily through springing suspensions and mechanisms to the trailer chassis so as to be in a fixed alinement with the longitudinal centerline of the trailer.
Rear overhang.- The rear overhang of a tractive truck, of a semitrailer, or of a full trailer is the distance between the centerline of the vehicle's rear axle and the centerline of its pintle hook.
Steering system.-One of two types of steering systems generally is used but related types are also used. The main ones are described in the following paragraphs.
- The Ackerman-steering system for front axles of power vehicles consists of a three-piece articulated axle with two front wheels that are mounted on short stub axles. The stub axles are attached to opposite ends of the rigid center section of the front axle by the front axle kingpins. The short stub axles are pivoted about the axle kingpins by steering arms and mechanisms connected to the driver's steering wheel.
- Fifth wheel pivot steering is similar to that used at the front ends of 2-axle, horse-drawn wagons. The front axle is a one-piece, rigid axle with the front wheels at each end of the axle. The rigid axle pivots about a kingpin located above the lateral center of the axle. Surrounding the kingpin are two lubricated bearing surfaces, the lower one is attached to the axle assembly. The upper hearing plate is attached to the underside of the rehicle chassis on its longitudinal centerline. These bearing plates give lateral and longitudinal stability to the cargo rehicle and make it possible for the trailer to be pulled by the kingpin. This type of steering is predominantly used at the front end of trailers.
- Pintle hook steering through a towbar is similar in action to fifth wheel pivot steering except that no vehicle weight rests on the pintle hook.


## Trailers.-There are three types of trailers:

- A semitrailer is a cargo trailer equipped with one or more axles at or near its rear; it is constructed so that a substantial part of its tare weight and its cargo weight rests upon a tractor through the tractor fifth wheel.
- A full trailer is basically a semitrailer that has been converted into a full trailer by one of two methods. In one method the front axle and spring suspension are permanently connected to the chassis of the trailer. In the other method a semitrailer is combined with a trailer converter dolly.
- A trailer converter dolly is a very short wheelbase semitrailer. It consists of an axle attached through a spring suspension system to a platform (chassis) that carries a lower fifth-wheel plate. It has a towbar mechanism affixed at 90 degrees to its axle. The front end of the towhar is equipped with a towing eye that engages with a pintle hook on the rear of the towing vehicle.

Toubar.-A towbar is a bar, or a V-shaped assembly two bars, attached to the chassis of a trailer converter do. or to the undetachable front axle assembly of a full trail and constructed so that it has a towing eye at its forwa end and exerts a pulling force in the middle of and a degrees to the axle of a trailer converter dolly or to a trailer undetachable front axle.
Turning path.-Turning path is the path of a designat point on a vehicle making a turn (2).
Turning radius.-The turning radius is the radius of circular turning path of the outside of the outer front $t$ from the turning radius center.
Turning radius center.-The turning radius center is t point that is the center of the circular turning path follow by the outside of the outer front tire of the power vehic
Turning track width.-The radial distance between $t$ turning paths of the outside of the outer front tire and $t$ outside of the rear tire nearest the center of the turn is $t$ turning track width (2).
ITheelbase.-The several measures of wheelbase, whi depend on the type of vehicle, are defined in the followi: paragraphs.

- The wheelbase of a single-unit power vehicle (tru or tractor) is the distance between the centerline of the fro axle and the centerline of the rear axle. The centerline 1 tween any tandem axles always is used as the reference poi for wheelbase measurements.
- On semitrailers, the wheelbase is the distance betwer
the trailer kingpin and the centerline of the rear axle.
- On trailer converter dollies, which are in effect sho semitrailers, the wheelbase is the distance between the cent of the towing eye of the towbar and the centerline of dolly's axle.
- The wheelbase of full trailers is measured the same wi as for semitrailers and is the distance between the kingp of the trailer and the centerline of the rear axle.
- On complete trailer combinations, the overall wheelba is the distance between the front axle of the power vehic and the rearmost axle when the trailer combination is stru out in a straight line. This overall wheelbase may dift from the sum of the defined wheelbases.
Width over tires.-The width over tires is the outside-t outside distance over the tires on an axle.

SAE definitions.-The meanings of the two following SA terms are different from the definitions and measuremen of offtracking that are used in this article. To prevel confusion the SAE definitions are given in the followin statements.
Turning center, SAE.-The turning center is the poin about which all parts of a vehicle or combination of vehicl revolve in describing a turn of constant radius and to whis all wheel spindles are normally radial. For 2-axled bogies tandems in which the axles are constrained to parallelis the interaxle trunnion or its equivalent is assumed to radial from this point (3). The location of this turnis center moves around as a trailer combination enters a cur from a tangent, procceds around the curve, and leaves an exit tangent. This turning center should not be fused with the outer front wheel turning radius cent referred to in this article.
Offtracking, SAE.-Offtracking is the difference in rac from the turning center to the vehicle centerlines at t. foremost and rearmost axles of a vehicle or combinati and represents the increase beyond the tangent track causi by a turn (3).
Peak offtracking.-Peak offtracking is the offtracking 1 sult obtained from the data shown in figure 5 and 6 . Tt peak offtracking may be equal to or less than the maximu offtracking calculated by use of SAE formulas.

## Fundamentals of Offtracking

Offtracking is the phenomenon in whic the paths of the wheels of a rear axde of single-muit power vehicle or of a trailer con bination deviate inward toward the ecenter a turn from the circular turning path of tl outside front wheel. When operating turns uniform in radius, individual vehicle whether in combinations or single-uni offtrack in similar patterns of tirns. Tl front wheels of a power unit do not offtrac but all other axles on the vehicle or trail combinations do. Although, most highwn vehicles have nonsteerable rear axles,


Figure 1.-A long wheelbase vehicle in tangent position about to enter turn.
all minority does have different methods rear steering. In the study discussed in s article only vehicles with nonsteering fur axles were studied.
For practical vehicle-highway geometries, most important factor of offtracking is offtracking that occurs when a singleit vehicle or a trailer combination makes turn of 270 degrees. On short wheelbase, - gle-unit vehicles, the peak offtracking may four early in the first 90 -degree segment of turn; but on very long trailer combinations, c full 270 degrees of turn may be used before te peak offtracking occurs. For the longer tiler combinations, the off tracking during 290-degree turn will be substantially less tan their offtracking on a 270 -degree turn. iso on 90 -degree turns, the front wheels of
the power vehicle of a long trailer combination will run for some distance on the exit tangent before the peak offtracking occurs. It is difficult to calculate the offtracking of trailer combinations having long wheelbases when the front wheels of the power vehicle travel on the exit tangent, but the solution can be obtained with scale models of vehicles. Of course, for very short wheelbase single-unit vehicles, which reach their maximum offtracking before 90 -degrees of turn, any travel on the exit tangent does not increase the amount of offtracking.

On turns, the offtracking characteristics of single-unit vehicles and the individual vohicles in trailer combinations are affected by several interlocking factors, such as: (1) the degree of a turn; (2) the wheelbase of each
individual vehicle in a trailer combination; (3) the uniform turning radius of the outside of the outer front tire of the power vehiclethis turning path of the outside of the outer front tire usually is the outer pavement or curb radius on a specific turn; (4) the radius of the outside of the outer front tire on a trailer's virtual front axle with reference to the turning radius center, when the towing vehicle is at its point of peak offtracking on a specific turn; (5) in trailer combinations, the rear trailing axle of each leading vehicle acts as a virtual front axle of the trailing vehicle.

The virtual front axles of trailing vehicles are: (1) on semitrailers, the tractor rear axle is the semitrailer's virtual front axle; (2) on trailer converter dollies or undetachable front axle assemblies of full trailers, the virtual front axle of such semitrailer-type assemblies is located on the centerline of the towing vehicle's pintle hook, which is the same locatimon as the center of the pintle hook eye of the towbar; (3) on full trailers the axle of the trailer converter dollies is the virtual front axle. However, on undetachable front-axle assemblies, such a front axle of a full trailer is its real front axle. Both types of front axles for full trailers perform similarly.

## Turning and Off tracking

## Single-unit vehicles

The principles of off tracking for single-unit vehicles are illustrated in figures 1 through 4, which show the action on turns of vehicles with Ackerman-stecring. A long single-unit vehicle is shown in figure 1 at its entrance tangent position just before entering a curve; the projections of the two stub axles of the front wheels and of the rear axle are parallel and do not intersect. For long vehicles, the projections of the front wheel, stub axles, and the rear axle vary from parallel when on the entrance tangent to different intersecting positions during a turn (fig. 2). The projectons reverse toward parallelism when the

igure 2.-A long wheelbase vehicle that has completed 90 degrees of turn but not reached peak off tracking.


Figure 3.-A long wheelbase vehicle at its point of peak off tracking on an exit tangent.
front wheels leave the turn on an exit tangent (fig. 3). Thus, the offtracking rear wheels travel in a double spiral curve.

The vehiele shown in figure 2 has not attained its peak offtracking on a 90 -degree turn; it is still in transition from its starting position even though the front wheels are at the exit tangent. Although, the projections of the stub axles of the front wheels pass through the turning radius center, the axis of the rear axle does not. In such situations, the peak offtracking will occur after the outer front tire of the rehicle is on its exit tangent (fig. 3). The front end of the vehicle has moved down the exit tangent until the projected axis of the rear axle passes through the turning radius center. This point of peak offtracking during it 90-degree turn was observed in the operation of the rehicle models. The axes of the front wheels no longer pass through the original turning radius center, but the axes of all axles will intersect at some distance behind the turning radius center. The amount of offtracking was measured with the vehicle modcls, but this offtracking cannot be calculated by use of the SAE equations.

For single-unit vehicles having short wheelbases, such as passenger cars and small trucks, maximum offtracking usually will occur during the first 90 -degree segment of a turn (fig. 4). As shown, the axes of all axles intersect at the turning radius center. The offtracking of such vehicles was measured with the vehicle models and results are shown in figures 5 and 6 . The offtracking of these short wheelbase vehicles also can be calculated by use of the SAE equations.

## Trailer combinations

It is desirable that trailer combinations move continuously and progressively forward at a reasonably rapid speed when negotiating highway curves or at-grade intersections. Becanse of their jointed construction, trailer combinations may not travel in a continuous, smooth path when the turning radius is shorter than the trailer wheelbase. Such nonuniform type of travel is possible with trailer combinations because fifth-wheel, pivottype steering permits a trailer to turn 90degrees or more from the longitudinal axle of the towing vehicle. The angle through which the power whicle can turn is limited by its stecring (ramp angle and its wheelbase.

An cexmple of a trater combination offtracking in a noncontimons, irregular manner is illustrated in figure 7 . As shown, when trailer combinations are negotiating 1 sto degree tums and the thrning radius is less than the length of the trailer's wheelbase, the reat aske will pats behincl the turning radins center and will pivot and travel backwarks in aln irregular path. The rear axle of long trailer combinations traveling On short radins, 27 ()-degree thrns also have similar backing and pivoting characteristics. Such reverse travel and pivoting of the rear axle c:an only be considered in very close quarters, for example, in buildings where the drivers carefully manipulate the trailer combinations at crecp speeds. Data in figures


Figure 1.-A short wheclbase vehicle that has reached its point of maximum off tracking.

5 and 6 do not apply to this type of irregular offtracking.

Trailer combinations negotiating 90-degree turns, however, travel in a continuous and smooth path regardless of which side of the turning radius center the semitrailer passes. A long wheelbase trailer combination following a relatively short turning radius, a situation truck drivers encounter as typical of city streets, is shown in figure 8. Because the outer rear tire on the rear axle passes behind the turning radius center, the maximum offtracking cannot be calculated with the SAE equations but can be and was measured with the vehicle models. The peak offtracking on such a turn occurs when the projection of the rear axle, as shown in figure 8 , passes through the turning radius center although the front wheels of the power vehicle are on the exit tangent. The problems associated with long trailer combinations negotiating curves having short turning radii are troublesome, particularly on city streets and diamond approaches to controlled-access highways. Such problems will be magnified if, in the future, longer single-trailer combinations are permitted. In general, double-trailer combinations offtrack less than long single-trailer combinations.

## Factors in Offtracking Determinations

An important feature of vehicle offtracking is that the peak offtracking for any clegree of smooth and continuous turn occurs when a projection of the axis of the rear axle of a vehicle is on a radial passing through the turning radius center. This was observed with the rehiele models, which were equipped with a seale that projected from the outer end of the trailing rear axle. The peak
outer rear tire offtracking occurred wt the rear axle was parallel with a radial 1 passing through the turning radius cen on the model test pattern.

The different measurements of offtrack data of interest and use to the highway des. engineer are: (1) Dimensions of vehic and trailer combinations; (2) turning rad of specified turn; (3) offtracking of trail rear axle; (4) turning track width; and inside curb radius, for zero clearance y tire.

## Dimensions

The dimensions of vehicles and tra combinations are needed so that the des engineer will know the sizes of vehicles be considered in a specific turn situati Dimensions needed of the individual vehis in a trailer combination are: wheelbase each vehicle, width over the tires; and double cargo vehicle combinations, the owrerhang of each towing vehicle and spacing between the vehicles.
The outer curb radius of a specific nsually is determined by the location terrain situation in the turning area. tracking is the radial distance between outer front where turning radius of the side of the outer front tire of a vehicle the radius of the ontside of the outer tire of a rear trailing axle, at the point peak offtracking. Offtracking for single-v vehicles and individual vehicles of tra combinations can be obtained from the tracking data in figures 5 and 6 .

The turning width is the amount of tracking plus the width over the tires of dual tires on a rear axle or the width of cargo body; if it is significantly wider tl the width over the dual tires. This dimens was :lssiumed to be 8.0 feet in the sth


Figure 5.-Offtracking and turning radii for 90-degree turns and different wheelbases.


Figure 6.-Offtracking and turning radii for 270 -degree turns and different wheelbases.


Figure 7.-A long wheelbase combination on a short radius turn, in which the semitrailer backs up and pivots behind the turning radius center.
sported here because it is the width presently lost in use. However, the 1965 A ASHO sze and Weight Recommendations carry a Iovision for over-the-tire widths of 8.5 feet. The inside pavement or curb radius on a irn is the radius from the turning radius inter to the outside of the innermost rear fe on the rear axle at the point of its peak stracking for a specific turn. The inside irb radius equals the original front-wheel irning radius minus the turning track width. 'his inside curb radius will permit a perfectly civen trailer combination, following the secified outer curb turning radius, to just ear the inner curb at its point of peak Itracking. The actual inner curb radius fould be shorter so as to permit variations i driver manipulation. The offtracking of idividual single-unit vehicles can be detrmined from the offtracking data in figures iand 6 by a single reference to either the ?-degree or the 270 -degree information.

## :ailer combination

The offtracking of a trailer combination on : specific turn is a summation of the offracking of the individual vehicles in the failer combination. Each vehicle in a trailer embination offtracks individually in accord-
ance with its wheclbase and the radius from the turning radius center to the outside of the outer front tire on its virtual front axle. Determining the turuing radius of the real or virtual outer front tire of each individual trailer vehicle in the train poses a problem. Because all trailing vehicles (semitrailers, trailer converter dollies, or undetachable full trailer, front-axle assemblies, and full trailers) offtrack and steer like semitrailers, a virtual or real front axle for each such semitrailer-like unit must be assumed. The point of peak offtracking for the rear axle of each towing vehicle on a specific turn will prescribe the turning radius of each following semitrailerlike unit. Proceeding from the front axle of a trailer combination, a progressive series of changed, usually reduced, turning radii occurs for the outer tire of the virtual front axle for each semitrailer-like unit. By analyzing each semitrailer-like unit in the order it appears in the trailer combination, using in sequence the turning radius of the outer front tire on each real or virtual front axle, it is possible to obtain a series of separate offtracking measurements for each vehicle. These measurements can be added to obtain the peak overall offtracking of the complete trailer combination.

When determining the offtracking of trailer combinations having full trailers, the phenom-
enon of negative offtracking must be considered. Negative offtracking oceurs when the edge of the cargo body opposite the pintle hook swings outside the path of the outside of the outer rear tire on a turn, as shown in figure 9. In effect, negative offtracking increases the turning radius of the following semitrailerlike unit. The magnitude of negative offtracking depends upon the wheelbase of the towing vehicle, the length of rear overhang to the centertine of the pintle hook, turning radius, and the degree of turn. The negative offtracking measurements for practical power vehicles and towing semitrailers are given in tables 1 and 2 .

## Steering Systems

## Ackerman steering

An understanding of different aspects of vehicle turning and offtracking requires information on the systems of steering used on most highway vehicles. Single-unit vehicles, automobiles, light trucks, tractive trucks, and tractors, are equipped with Ackerman-type steering. The Ackerman system was invented in Germany about 1817 and patented by an Englishman in 1818. It is the preferred steering system because it provides better stability to the front end of the vehicle during a turn. In the Ackerman system the two front wheels are mounted on short, stub axles that are connected to the steering kingpins. The kingpins are connected to the front-wheel spring suspension and are supported by the vehicle chassis or sometimes by a rigid beamtype front axle. During a turn, the front wheels are pivoted on the kingpins by the steering linkage and other mechanisms connected to the steering wheel.

Vehicles equipped with Ackerman steering are limited in their offtracking by the minimum turning radius curve that can be followed by the outer front wheel. This minimum turning radius usually is limited, because of mechanical obstructions, by the degree to which the inner front wheel may be turned. This limited turning capability of the immer front whecl is called the cramp angle. On most over-the-road trucks the maximum cramp angle is between 30 and 35 degrees. Re:cently, however, the manufacturers of city delivery trucks have been widening the distance between front wheels and are obtaining cramp angles of 45 to 50 degrees. Offtracking data for such vehicles are included in the figures in this article.

## Fifth-wheel steering

Semitrailers, full trailers, and trailer converter dollies operate with a fifth-wheel, pivotsteering principle that is different from the Ackerman system. As trailers are not operated alone, they do not require the front-end stability required for power vehicles. In the fifth-wheel, pivot-type of steering system the front wheels are mounted at the ends of a rigid one-piece axle. This axle is pivoted about a kingpin mounted above the lateral center of the axle, where it is comnected to the trailer body.


Figure 8.- A long wheelbase combination on a short radius turn, in which the semitrailer passes in back of the turning radius center.


Figure 9.-Negative offtracking in which the path of the ou rear corner of the cargo body has a greater radius than the $p$, of the outer rear wheel.

For semitrailers the rear axle of the tractor acts as the virtual front axle of the trailer. In most designs, the trailer kingpin, surrounded by a lubricated bearing plate, is attached to the maderside of the semitrailer, usually about 3 feet back of the front end of the trailer. Another bearing plate, equipped with a kingpin locking device, is mounted on the tractor chassis over the rear axle. This fifth wheel engages and holds the trailer kingpin and allows the trailer to be pulled and steered by the 1 ractor. This system permits easy coupling or uncoupling and the interchanging of trailers.

Full trailers are basically semitrailers that have one or two types of front-axle assemblies; the front axle is permanently attached to the trailer or is removable. The removable, front-anle assemblies are known as trailer converer dollies. They consist of one or more one-piece axles supported by a spring suspension system and have a fifth wheel mounted above the center of the axle. Both the trabler converter dollies and the permanently attached front-asle assemblies have towbars affixed at a 90 -degree angle to the axle. The towhar has an eve that engages a vertical pintle hook on the rear of its towing rehicle. Oncer engiged, the towbar may pivot freely about its pintle hook. Such pivoting is limited only by interferences with rear frame parts of the towng vehicle. Becanse of the free pivoting action of the towbar, both types of front-axle asemblies of full trailers act as short wheelbase semitrailers in making at turn. Thus a full trailer turns and offtracks in the same mannere ats a semitrater commeted in
tandem to another semitrailer, both of which have fifth-wheel pivot steering.

In the steering and offtracking behavior of full-trailer front-axle assemblies, their virtual front axle can be assumed to be located at the center of the pintle hook. The wheelbase of such devices, therefore, is measured from the center of the towbar eye to the center of the axle. With fifth-whecl-pivot steering no cramp-angle problem occurs and the angular relationship between the towing vehicle and the semitraler is not restricted; it may be as much as or more than 90 degrees.

## Vehicle Models and Instrumentation

The relations on offtracking contained in this article were obtaned primarily through the use of scale morlels of highway vehicles. The models were designed to provide a good simulation of actual vehicle tuming characteristies for many different types and lengths of single-mnit vehicles and trater combinations. To expedite the study, models were designed as detachable components that could be quickly assembled or disassembled. The models, equipperl with an Ackerman steering mechanism, were constructed to a seale of 0.75 inch equals 1 foot and the widt h over the tires equals 8 model feet.

The models were operated on a smooth surface of 4 -by-S-foot panels placed on a level concrete floor. The panels were assembled in 16-by-16-foot squares and circless were painted from the center to simulate
highway curves ranging from a turning $r$ of 25 to 100 model feet. Radial lines, 10-degree intervals, and tangents were su imposed upon the test layout, as showr figure 10. Turning radii of 165 and 225 m feet were obtained by placing 8 additi, panels about the original 16 -by-16-foot squ

Before each individual test, the vel and axle alinement of the model was chec on an 8 -foot approach tangent. If the $m$ followed the tangent without any per tible deviation, it was then guided so that outside of the outer front wheel followed circular curve selected for the test. Offtr ing tests were conducted with morlels re senting different types of single-unit vehicles trailer combinations. Included were mode power vehicles with wheel bases ranging 1 5 to 30 model feet, tractive truck models considerable rear overhang, and semitr models with wheelbases ranging from 55 model feet. Full trailer model were not condueted as full trailers offt the same way as semitrailers.

In the semitrailer model tests the tr kingpin was positioned directly over the center of the front axle of a short w base tractor model, as shown in figurel With the kingpin in this position any tracking of the tractor did not affect trailer offtracking; however, the tractor provicle model stability. In all of the ml tests the offtracking was measured at rear or trailing axle of a vehicle or tr combination. To ascertain the magni of negative offtracking on tractive t
ving long rear owerhangs, all additional tracking measurement was taken at the ter rear comer of the morlel opposite the itle hook eenterline. To expedite the termination of the peak offtracking, a scale \& momiter on the vehicle models as shown figtre 11. Offtracking data were obtained the model assemblies for both $90-$ and o-degree tums.

## Offtracking Calculations

The results obtained from the tests on hicle models are shown in figures 5 and 6 - 90 degree turns. They were designed permit the rapid determination of offleking for single-unit vehicles and trailer mbinations. For single-unit vehicles, the tracking can be determined directly. Deimination of the offtracking for trailer imbinations can be obtained by adding tother the offtracking of the individual units the combinations. Semilogarithmic graph pper was used in the preparation of these foures. The ordinate in a logarithmic scale presents offtracking in feet. The logarithie scale was selected to reduce the height of te ordinates for publication. The abscissa presents the turning radius in feet and it has sen presented on an equal interval scale. i each figure, the wherlbase curves were awn in 5-foot increments.
Vehicle offtracking may be evaluated for uning radii of 25 to 225 feet and for wheelase lengths of 5 to 55 feet. The 25 -foot uning radius represents the shortest radius irn studied with the models. At more than 225 -foot turning radius, the offtracking of ngle-unit rehicles and trailer combinations pproaches the maximum offtracking that min be calculated by the SAE equations (1). ; he approximate limits of the minimum radii f turns possible when an Ackerman-type leering system is employed and when the ont wherl cramp angle is 50 degrees are flso shown. The following examples exlain how the data in these figures can be sed.

## ingle-unit vehicles

The offtracking for single-unit vehicles can lale determined directly. For example, the de eak offtracking for a 2 -axle truck negotiating turning radius of 70 feet on a 90 -degree urn is shown in figure 5 . If the 2 -axle ruck had a wheelbase of 30 feet, the peak fffracking would be 6.4 feet. If the same -axle truck was negotiating a 70 -foot radius furve through a 270 -degree turn, the peak Iffracking would be 7.0 feet (fig. 6). If The minimum turning radius for the 2 -axle fruck is desired, it can be approximated by rise of the dashed curve shown on the figure. f the front wheel cramp angle is 50 degrees, a rB0-foot wheelbase, single-unit truck eannot regotiate a curve having a turning radius of ess than 45 feet (fig. 5).
If the offtracking is desired for a vehicle thaving a wherlbase between those reprertisented by the wheelbase curves in either affigure 5 or 6 , figure 12 may be used to interrpolate between the whedbase curves. For example, if offtracking had been desired for a


Figure 10.-Schematic arrangement of guidelines on floor panels.


Figure 11.-Semitrailer model and fifth-wheel pivot steering.

Table 1.-Negative offtracking for 90 -degree turns

| $\begin{aligned} & \text { Wheel- } \\ & \text { hase } \end{aligned}$ | Turning rarlius of outsicie of outer front u heel | Offtracking of outsirle of outer rear wheel | Negative offtracking of outer rear corner opposite pintle hook for- |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{aligned} & 3 \text {-foot } \\ & \text { overhang } \end{aligned}$ | $\begin{gathered} 5 \text {-foot } \\ \text { overhang } \end{gathered}$ | $\left\|\begin{array}{c} 7 \text {-foot } \\ \text { overhang } \end{array}\right\|$ | 9-foot overhang | $\text { \| } \begin{gathered} 11-\text { foot } \\ \hline \end{gathered}$ |
| $\begin{gathered} \text { Fet } \\ 10 \end{gathered}$ | $\begin{array}{r} \text { Fect } \\ 25 \\ 30 \\ 10 \\ 50 \\ 60 \\ 70 \\ 70 \\ 80 \\ 90 \\ 100 \end{array}$ | Feet 2. 10 1. 71 1. 27 1. 01 .85 .75 .76 .60 .54 .54 | Feet 0.19 $.1 ;$ .12 .00 .00 .00 .00 .00 .00 | $\begin{array}{r} \text { Feet } \\ 0.54 \\ .44 \\ .32 \\ .26 \\ .21 \\ .18 \\ .16 \\ .15 \\ .13 \end{array}$ | Feet 1.04 .85 .63 .50 .41 .35 .31 .27 .25 | Feet 1.70 1.40 1.03 .82 .68 .58 .51 .45 .39 | Feft |
| 15 | $\begin{array}{r} 25 \\ 30 \\ 40 \\ 50 \\ 50 \\ 610 \\ 70 \\ >0 \\ 90 \\ 90 \\ 100 \end{array}$ | $\begin{aligned} & 3.62 \\ & \text { 3. } 24 \\ & \text { 2. } 70 \\ & \text { 2. 30) } \\ & \text { 2. } 00 \\ & \text { 1. 75 } \\ & \text { 1.55 } \\ & \text { 1. } 38 \\ & 1.23 \end{aligned}$ | .20 .17 .12 .00 .00 .00 .00 .00 .00 | $\begin{aligned} & .55 \\ & .46 \\ & .33 \\ & .26 \\ & .22 \\ & .18 \\ & .16 \\ & .14 \\ & .13 \end{aligned}$ | $\begin{array}{r} 1.11 \\ .88 \\ .64 \\ .51 \\ .42 \\ 36 \\ .31 \\ .28 \\ .25 \end{array}$ | $\begin{array}{r} 1.78 \\ 1.45 \\ 1.07 \\ .81 \\ .69 \\ .59 \\ .51 \\ .46 \\ .41 \end{array}$ | $\begin{array}{r} 2.75 \\ 2.17 \\ 1.59 \\ 1.25 \\ 1.03 \\ .88 \\ .77 \\ .68 \\ .61 \end{array}$ |
| 20 | $\begin{array}{r} 25 \\ 30 \\ 40 \\ 50 \\ 60 \\ 70 \\ 80 \\ 90 \\ 100 \end{array}$ | $\begin{aligned} & \text { 5. } 13 \\ & \text { 5. } 05 \\ & \text { 4. } 40 \\ & \text { 3. } 89 \\ & \text { 3. } 45 \\ & \text { 3. } 08 \\ & \text { 2. } 72 \\ & \text { 2. } 41 \\ & 2.17 \end{aligned}$ | $\begin{array}{r} .22 \\ .18 \\ .13 \\ .10 \\ .00 \\ .00 \\ .00 \\ .00 \\ .00 \end{array}$ | $\begin{array}{r} .62 \\ .51 \\ .51 \\ .35 \\ .22 \\ .19 \\ .16 \\ .14 \\ .13 \end{array}$ | $\begin{array}{r} 1.23 \\ .96 \\ .68 \\ .53 \\ .43 \\ .37 \\ .32 \\ .28 \\ .25 \end{array}$ | $\begin{array}{r} 1.96 \\ 1.56 \\ 1.12 \\ .87 \\ .71 \\ .60 \\ .52 \\ .46 \\ .41 \end{array}$ | $\begin{array}{r} \text { 2. } 97 \\ 2.33 \\ 1.665 \\ 1.29 \\ 1.15 \\ \text { 1. } 15 \\ .90 \\ .78 \\ .69 \\ .62 \end{array}$ |
| 25 | $\begin{array}{r} 25 \\ 30 \\ 40 \\ 40 \\ 50 \\ 60 \\ 70 \\ 80 \\ 80 \\ 90 \\ 100 \end{array}$ | $\begin{aligned} & \text { 8. } 37 \\ & \text { 7. } 80 \\ & \text { 6. } 80 \\ & \text { 5. } 93 \\ & \text { 5. } 28 \\ & \text { 4. } 61 \\ & \text { 4. } 10 \\ & \text { 3. } 70 \\ & \text { 3. } 34 \end{aligned}$ | 27 .20 .14 .10 .00 .00 .00 .00 .00 | $\begin{array}{r} .74 \\ .74 \\ .58 \\ .37 \\ .28 \\ .23 \\ 19 \\ 16 \\ .14 \\ .13 \end{array}$ | $\begin{array}{r} 1.43 \\ 1.08 \\ .73 \\ .55 \\ .45 \\ .37 \\ .32 \\ .28 \\ .25 \end{array}$ | $\begin{array}{r} 2.28 \\ 1.75 \\ 1.20 \\ .91 \\ .74 \\ .62 \\ .53 \\ .47 \\ .42 \end{array}$ | $\begin{array}{r} 3.31 \\ 2.58 \\ 1.77 \\ 1.35 \\ 1.09 \\ .92 \\ .79 \\ .70 \\ .62 \end{array}$ |
| 30 | $\begin{array}{r} 25 \\ 30 \\ 30 \\ 40 \\ 50 \\ 60 \\ 70 \\ 80 \\ 90 \\ 900 \\ 100 \end{array}$ | $\begin{array}{r} 11.71 \\ 10.90 \\ 9.50 \\ 8.30 \\ 7.27 \\ 6.41 \\ 5.70 \\ 5.11 \\ 4.62 \end{array}$ | $\begin{array}{r} .33 \\ .23 \\ .15 \\ .11 \\ .00 \\ .00 \\ .00 \\ .00 \\ .00 \end{array}$ | .92 .66 .41 .30 .24 .20 .17 .15 .13 | $\begin{array}{r} 1.76 \\ 1.24 \\ .79 \\ .58 \\ .46 \\ .38 \\ .33 \\ .29 \\ .26 \end{array}$ | $\begin{array}{r} 2.73 \\ 2.01 \\ 1.30 \\ .96 \\ .76 \\ .63 \\ .55 \\ .48 \\ .42 \end{array}$ | $\begin{array}{r} 3.96 \\ 2.94 \\ 1.92 \\ 1.43 \\ 1.14 \\ .94 \\ .81 \\ .71 \\ .63 \end{array}$ |
| 35 | $\begin{array}{r} 25 \\ 30 \\ 40 \\ 50 \\ 60 \\ 70 \\ 80 \\ 40 \\ 100 \end{array}$ | $\begin{array}{r} 15.08 \\ 14.20 \\ 12.55 \\ 11.10 \\ 9.660 \\ 8.49 \\ 7.52 \\ 6.72 \\ 6.10 \end{array}$ | $\begin{array}{r} .44 \\ .28 \\ .16 \\ .12 \\ .00 \\ .00 \\ .00 \\ .00 \\ .000 \end{array}$ | 1.19 .77 .46 .32 .25 .20 .17 .15 .13 | $\begin{array}{r} 2.22 \\ 1.48 \\ .88 \\ .62 \\ .48 \\ .30 \\ .38 \\ .29 \\ .26 \end{array}$ | $\begin{array}{r} 3.47 \\ 2.38 \\ 1.44 \\ 1.04 \\ .80 \\ .65 \\ .56 \\ .49 \\ .43 \end{array}$ | $\begin{array}{r} \text { 4. } 89 \\ 3.45 \\ 2.12 \\ 1.53 \\ 1.19 \\ .98 \\ .83 \\ .72 \\ .64 \end{array}$ |

Table 2. - Negative offtracking for 270-degree turns

| Wheelbase | Turning radius of outside of outer front wheel | Offtracking of outsi/le of nuter rear wheel | Negative offtracking of outer rear corner opposite pintle hook for- |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{gathered} 3-\text { foot } \\ \text { overhang } \end{gathered}$ | $\begin{gathered} 5 \text {-foot } \\ \text { overhang } \end{gathered}$ | $\begin{gathered} 7 \text {-foot } \\ \text { overhang } \end{gathered}$ | $\begin{gathered} 9 \text {-foot } \\ \text { overhang } \end{gathered}$ | $\begin{gathered} 11-\text { foot } \\ \text { overhang } \end{gathered}$ |
| Feet 10 | Feet | Feet | Feet | Feet | Feet | Feet | Feet |
|  | 25 | 2. 58 | 0. 20 | 0. 55 | 1. 07 | 1. 74 |  |
|  | 30 | 1.90) | . 16 | . 44 | . 8 4 | 1. 41 |  |
|  | 40 | 1. 27 | . 12 | 32 | 63 | 1. 03 |  |
|  | 50 | 1. 01 | . 00 | 25 | 50 | . 82 |  |
|  | 60 | . 85 | . 00 | 21 | 41 | , 8 |  |
|  | 70 | 75 | . 00 | . 18 | 35 | . 58 |  |
|  | 80 | . 67 | . 00 | . 16 | 31 | . 51 |  |
|  | 90 | . 60 | . 00 | . 14 | 27 | . 45 |  |
|  | 100 | . 54 | . 00 | . 13 | 25 | 41 |  |
| 15 | 25 | 10.40 | . 31 | . 83 | 1.59 | 2. 55 | 3. 68 |
|  | 30 | 4. 60 | . 18 | . 49 | . 95 | 1. 55 | 2. 28 |
|  | 40 | 3. 43 | 12 | . 33 | 67 | 1. 09 | 1. 63 |
|  | 50 | 2. 68 | , 00 | . 26 | . 51 | . 85 | 1. 26 |
|  | 60 | 2. 18 | . 00 | . 22 | . 12 | . 70 | 1. 03 |
|  | 70 | 1. 83 | . 00 | . 18 | . 36 | . 59 | . 88 |
|  | 80 | 1. 61 | . 00 | . 16 | . 31 | . 51 | . 77 |
|  | 90 | 1.38 | . 00 | . 14 | . 28 | . 46 | . 18 |
|  | 100 | 1. 23 | . 00 | . 13 | . 25 | . 41 | .61 |
| 20 | 25 | 18.93 | . 70 | 1. 79 | 3. 19 | 4. 79 | 4. 49 |
|  | 30 | 8.70 | . 21 | . 58 | 1. 12 | 1. 82 | 2. 67 |
|  | 40 | 6. 24 | . 13 | . 37 | . 72 | 1.18 | 1. 75 |
|  | 50 | 4. 72 | . 10 | . 27 | . 54 | . 89 | 1.30 |
|  | 60 | 3. 71 | . 00 | . 22 | . 43 | . 71 | 1. 06 |
|  | 70 | 3.10 | . 10 | . 19 | . 37 | . 60 | . 90 |
|  | 80 | 2. 73 | . 00 | . 16 | . 32 | . 52 | . 78 |
|  | 90 | 2.41 | . 00 | . 14 | . 28 | . 44 i | . 69 |
|  | 100 | 2. 17 | . 00 | . 13 | . 25 | . 11 | . 62 |
| 25 | 25 |  | - | -77- |  |  |  |
|  | $\pm 0$ | 14. 25 | . 28 | . 77 | 1.55 | 2. 39 | 3. 46 |
|  | 40 | 9. 70 | . 15 | . 41 | . 80 | 1. 31 | 1. 93 |
|  | 50 | 7. 27 | . 11 | . 29 | . 57 | . 95 | 1.39 |
|  | 60 | 5. 81 | . 00 | . 23 | . 45 | . 74 | 1.10 |
|  | 70 | 4. 81 | . 00 | . 19 | . 7 | . 62 | . 92 |
|  | 80 | 4. 17 | . 00 | . 16 | . 32 | . 53 | . 79 |
|  | 90 | 3. 70 | . 00 | . 14 | . 28 | . 47 | . 70 |
|  | 100 | 3.34 | . 00 | . 13 | . 25 | . 42 | . 12 |
| 30 | 25 |  |  |  |  |  |  |
|  | 30 | 26. 01 | 1. 00 | 1. 80 | 4.07 | 5. 85 | 7.71 |
|  | 40 | 14.85 | . 18 | . 49 | . 88 | 1. 52 | 2. 20 |
|  | 50 | 11. 21 | . 12 | . 32 | . 63 | 1. 03 | 1. 53 |
|  | 60 | 8. 67 | . 00 | . 24 | . 48 | . 78 | 1.17 |
|  | 70 | 7. 18 | . 00 | . 20 | . 39 | . 64 | . 96 |
|  | 80 | 6. 07 | . 00 | . 17 | . 33 | . 55 | . 81 |
|  | 90 | 5. 26 | . 00 | . 15 | . 29 | . 48 | . 71 |
|  | 100 | 4. 70 | . 00 | . 13 | . 26 | . 42 | . 63 |
| 35 | 25 30 | 38. 00 | ------ | ------ | ------ | ---..- |  |
|  | 40 | 18.80 | -20) | . 58 | 1. 13 | 1.83 | 2. 68 |
|  | 50 | 15. 655 | . 13 | . 36 | . .71 | 1. 16 | 1.72 |
|  | 60 | 12. 50 | . 00 | . 26 | . 51 | . 85 | 1. 24 |
|  | 70 | 10. 15 | . 00 | . 21 | . 41 | . 67 | 1.00 |
|  | 80 | 8. 50 | . 00 | . 17 | . 34 | . 56 | . 84 |
|  | 90 | 7.35 | . 00 | . 15 | . 30 | . 49 | . 73 |
|  | 100 | 6. 57 | . 00 | . 13 | . 26 | . 43 | . 6.5 |

single-mit truck having a 11 -foot wheelbase the following procedure would be employed. Use the vertical distance from figure 5 or figure 6 between the 10 - and 15 -foot wheelbase curves and locate the same distance vertically on figure 12 between the 10 - and 15 -foot lines. It this location, the vertical distance between the 10- and 11 -foot lines is then carried back to figure 5 or 6 and located vertically above the 10 -foot wheelbase curve; the offtracking is then read on the ordinate horizontally opposite the point representing the 11 -foot wheelbase. When negotiating a 90 -degree turn, the peak offtracking for this single-unit vehicle would be 0.9 foot.

## Tractor combinations

Offtracking is determined for tractor semitrailers by adding the offtracking data for the individual vehicles of the combinations. For example, the peak offtracking for a $2-\mathrm{S} 2$ combination negotiating a turning radius of 100 feet through a 270 -degree turn would be de-
termined from figure 6 . The dimensions of the sample $2-\mathrm{S} 2$ trailer combination are given in figure 13 . The peak offtracking is determined for the tractor having a 10 -foot wheelbase ( 0.54 foot, fig. 6). To determine the semitrailer offtracking, its turning radius and wheelbase must be known. The assumption has been made that the kingpin is located directly above the centerline of the rear axle of the tractor (figs. 5 and 6). In effect, the rear axle of the tractor becomes the virtual front axle of the semitrailer. The semitrailer turning radius is computed by subtracting the tractor offtracking from the tracking turning radius; it is 99.5 feet. The semitrailer wheclbase is the distance from the kingpin to the centerline of the rear axle on the semitrailer. In this example, the semitrailer had a tandem rear axle, therefore, the wheelbase of 29 feet is the distance from its kingpin to the centerline between the tandem axles. Reference to figure 6 shows the semitrailers peak offtracking was 4.4 feet when the turning radius was 99.5 feet and the
wheelbase was 29 fect. The offtracking $f^{\prime}$ the tractor-semitrailer portion of the trail combination is the sum of the tractor of tracking and the semitrailer offtracking ( 0 . plus 4.4 or 4.94 feet). As previously dete mined, the tractor semitrailers peak of tracking, in reference to the centerline betwer the tandem axles, was $4.9 \pm$ feet when neg. tiating a 100 -foot turning radius through 2 ; degrees. But the offtracking for the trail converter dolly and the full trailer also mu be determined.

The trailer converter dolly is connected the semitrailer at a pintle hook, located 7 fe behind the canterline between the tande: axles. Negative offtracking is present in thi the path of the outer rear corner of the sem trailer swings outward from the turning radir center. The magnitude of negative offtracl ing can be determined from table 1 or With a wheelbase of approximately 30 fee a turning radius of nearly 100 feet, and 7 -foot rear overhang to the pintle hook, tl

;ure 12.-Interpolation guide for wheelbase lengths between 5-foot interval wheelbase curves.


Figure 13.-Dimensions of trailer combination used to demonstrate calculations.
lgative offtracking of the virtual front axle the dolly is 0.26 foot for a 270 -degree turn. The pintle hook was assumed to be in the nter of the virtual front axle of the trailer inverter dolly. The trailer converter dolly trning radius is found by subtracting the actor semitrailer offtracking ( 4.94 feet) from he turning radius of the tractor and adding di) that the negative offtracking. Thus, the Arning radius of the virtual front axle of the "ailer converter dolly would be 95.32 feet 00.00 minus 4.94 plus 0.26 ). With the trailer onverter dolly having a wheelbase of 7 feet
and a turning radius of 95.32 feet, the dolly offtracking of 0.28 foot, was determined from figure 6.

After the peak offtracking of the trailer converter dolly is obtained, the offtracking for the full trailer is determined. The turning radius for the full trailer is computed in the same way as for the semitrailer. Thus, the turning radius of the virtual front axle of the full trailer is 95.04 feet ( 95.32 minus 0.28 ). The kingpin on the full trailer is assumed to be directly above the centerline of the dolly axle. If a tandem axle dolly had been used,
the kingpin would be located directly above the centerline between the tandem axles. In effect the dolly axle is the virtual front axle of the full trailer. For a full trailer having wheelbase of 24 feet and a turning radius of 95.04 feet, the full trailer offtracking is 3.2 feet (fig. 6).

The offtracking of the entire 2-S2-2 tractor semitrailer and full trailer with an overall length of 83 feet is the sum of the offtracking of the individual vehicles mimus the negative offtracking. The peak offtracking for the 2-52-2 combination example would be 8.16 feet $(0.54+4.40+0.28+3.20-0.26)$ when negotiating a 100 -foot turning radius curve through a 270 -degree turn. The turning track width would be 16.16 feet $(8.16+8.00)$. The inside curb radius is equal to the turning radius minus the turning track width or 83.84 feet ( $100-16.16$ ). The computed SAE maximum offtracking for this vehicle is 8.42 feet.

## Truck and full trailers

The peak offtracking for truck and full trailers also can be determined by use of data shown in figures 5 and 6 . The same techniques are used for determining the offtracking of the individual vehicles of a truck and full trailer combination as are used for determining the offtracking of a tractor semitrailer and full trailer combination.

## Offtracking Comparisons

To illustrate that different types and sizes of vehicle combinations offtrack differently, several representative long trailer combinations were selected for comparisons. Dimensions of the trailer combinations are listed in table 3 and offtracking characteristics are listed in table 4 . In table 3, the 2-S1, $2-\$ 2$, and $3-\$ 2$ combinations have over-all lengths shorter than either of the $2-S 1-2$ combinations listed. However, the 65 -foot, 2-S1-2 combination offtracks less than either of the tractor-semitrailer combinations and the 71-foot $2-\$ 1-2$ combination has approximately the same offtracking as the tractor semitrailers. Because vehicles do offtrack differently; highway design engineers use as guides the highway design vehicles recommended by the American Association of State Highway Officials. The offtracking characteristies given for vehicles in the 1965 proposed revision of the AASHO highway design vehicles also are shown in table 4. The dimensions proposed for these design vehicles are given in table 5.

## Model and S.1E Offtracking Comparisons

Offtracking results computed from tests with the models were compared to results obtained from the SAE offtracking equations. Comparisons were made for 90 - and 270 -degree turns on 50 - and 150 -foot turning radii, respectively. Most of the vehicle models obtained their maximum offtracking prior to reaching the 270 -degree exit tangent, thercfore, the results could be validated by com-
'rable ?. - Dimensions of some of the trailer combinations listed in table 4

|  | 2-81 | 2-S2 | $3-52$ | 2-S1-2 | $2-$ - $1-2$ | 3-S2-4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Feet | Feet | Feet | Fet 1 | Feet | Fept |
| Length of each trailer | 40 | 40 | 40 | 27 | 30 | 40 |
| Front humper to nose of first trailer. | 14) | 15 | 15 | 8 | 8 | 1 fi |
| Space between trailers .-.----..- |  |  |  | 3 | 3 | 3 |
| Wiuthover tires_---.... | 8 | 8 | 8 | 8 | 8 | 8 |
| Wheel hase, tractor (to centerline of tandem axle) | $11)$ | 15 | 1.5 | 8 | $\delta$ | 16 |
| Front bumper to front axle of tractor | 3 | 3 | 3 | 3 | 3 | 3 |
| Wherlhase, semitrailer | 3.1 | 29 | 32 | 21 | 21 | 32 |
| Rear pintle hook orerhang of semitrailer |  |  |  | 3 | 3 | 5 |
| Wheclbase of trailer converter dolly .-- |  | -..- | --. | 6 | 6 | 6 |
| Wheelbase, full trailer |  |  |  | 21 | 24 | 32 |
| Rear overhang of trailer | 3 | 8 | 5 | 3 | 3 | 5 |
| Overall length of trailer combinations . | 50 | 55 | 55 | 65 | 71 | 99 |

Table 4.-Vehicle offtracking computations and A ASIIO propos

| Vehicle types | $\begin{aligned} & \text { Over- } \\ & \text { all } \\ & \text { length } \end{aligned}$ | 90 -degree turn, 50 -foot turning radius |  |  | 270-degree turn, 150-foo turning radius |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Off-tracking | Turning track width | $\begin{aligned} & \text { Inside } \\ & \text { curt } \\ & \text { ractius } \end{aligned}$ | Off- <br> tracking | Turning track width | $\begin{aligned} & \text { Insic } \\ & \text { curt } \\ & \text { radii } \end{aligned}$ |
| Long trailer <br> combinations: | Feet | Feet | Feet | Feet | Feet | Feet | Fee |
|  | 50 | 11.3 | 19.3 | 30.7 | 4. 5 | 12.5 | 137. |
|  | 55 | 10.3 | 18.3 | 31.7 | 3. 7 | 11.7 | 135. |
|  | 55 | 11.7 | 19.7 | 30.3 | 4.3 | 12.3 | 137. |
|  | t5 | 9.4 | 17.4 | 32.6 | 3.3 | 11.3 | 138. |
|  | 71 | 12. 5 | 20.5 | 30.5 | 4.4 | 12.4 | 137. |
|  | 99 | 22.0 | 30.0 | 20.0 | 8.1 | 16. 1 | 133. |
| AASIIO proposals Passenger cars Ot her vehicles:$2-\mathrm{S} 2$$3-\$ 2$ | 19 | 1.1 | 7.1 | 42.9 | 0.4 | 6.4 | 113. |
|  |  |  |  |  |  |  | 17. |
|  | 30 | 3.8 | 12.3 | 37.7 | 1.2 | 9.7 |  |
|  | 50 | 7.8 | 16.3 | 33.7 | 2.7 | 11.2 | 138. |
|  | 55 | 11.8 | 20.3 | 29.7 | 4.2 | 12.7 | 137. |

${ }^{1}$ Proposerl 1965 revision of AASHO highway design vehicles.

Table 5.-Dimensions in proposed 1965 revision of AASHO highway design vehicles listed in table 4

|  | Singleunit truck or bus | 2-S2 <br> trailer <br> combi- <br> nations, <br> W B-401 | 3-S2 <br> trailer <br> combi- <br> nations, <br> W $13-501$ |
| :---: | :---: | :---: | :---: |
| Length of trailer. | Feet | Feet <br> 36 | Feet <br> 37 |
| Front bumper to nose of trailer.. |  |  | 18 |
| Width over tires......- | 8.5 | 8.5 | 8.5 |
| Wheelbase, single-unit truck, or tractor | 20 | 13 | 18 |
| Front bumper to front axle | 4 | 4 | 3 |
| Wheelbase, semitrailer |  | 25 | 30 |
| Rear overhang. | 6 | 8 | 4 |
| Overall length of vehicles. | 30 | 50 | 55 |

base.

Table 6.-Motel and SAE offtracking test results

| Trailer com-binations | Trailer length | $\begin{gathered} 0 \text { ver- } \\ \text { all } \\ \text { length } \end{gathered}$ | Offtracking |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 90 -degree turn, 50-foot turning radius |  | 270-degree turn, 150-foot turning radiu |  |
|  |  |  | Model | SAE | Model | SAE |
|  | Feet | Fect | Feet | Feet | Feet | Fect |
| - | $4{ }^{4}$ | $51)$ | 11. 30 | 16.62 | 4. 47 | 4.36 |
| 2- $\because 2$ | 411 | 55 | 13. 00 | 18.75 | 4. 96 | 4. 81 |
| 2- 2 | 411 | 515 | 8. 90 | 11.69 | 3.28 | 3. 26 |
| 2-s1 | $41)$ | 55 | 10. 30 | 13.51 | 3.72 | 3. 69 |
| $3-2$ | 10 | 51) | 10. 00 | 14.46 | 3.87 | 3. 90 |
| 3-s2 | 411 | 5 | 11.65 | 16.45 | 4.30 | 4.34 |
| 2- $-1-2$ | $2 \times 25$ | +i5 | 9.38 |  | 3. 28 | 3. 114 |
| 2-1-2 | $2 \times 30$ | 71 | 12. 48 |  | 4.41 | 4.32 |
| $3-2{ }^{2}$ | $2 \times 40$ | 94 | 21.97 |  | 8.12 | 8.16 |

paring them with the maximum offtracking results computed by the SAE equations. Results of some of the comparisons are listed in table 6. As shown the tractor-semitrailer models negotiating the 90 -degree turns on the 50 -foot turning radius curve did not obtain SAE maximum offtracking. For the tractorsemitrailer and full trailer models negotiating the same turns, the SAE offtracking equation is not applicable because the trailing rear axle of the trailer combination passed behind the turning center.

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[^1]:    $=2$-axle single-unit truck.
    $=3$-axle single-unit truck.
    $=2$-axle truck-tractor with 1 -axle semitrailer.
    $=2$-axle truck-tractor with 2 -axle semitrailer.
    $=3$-axle truck-tractor with 2 -axle semitrailer.
    $=2$-axle truck with 1 -axle trailer.
    $\equiv 2$-axle truck with 2 -axle trailer.
    $=3$-axle truck with 2 -axle trailer.
    $=4$-axle truck-tractor with 6-axle trailer.

[^2]:    ${ }^{1}$ All refers to the total number of vehicles tested in each category, regardless of brake system type or capacity group.

[^3]:    ${ }^{1}$ All refers to total number of vehicles tested in each category, as identified in table 5. ${ }^{2}$ Measured by pendulum-type decelerometer.

[^4]:    ${ }^{1}$ Includes 3-82 and 2-81-2 and other trailer combinations not listed specifically.

[^5]:    Presented at the 4 th annual meeting of the Highway
    esearch Board, Washington, D.C., Jan. 1965.

[^6]:    ${ }^{2}$ References indicated by italic numbers in parentheses are listed on page 100.

